

When Priority Values Change ①

Suppose one item in a Max-Heap changes its value. If the value increased, it may be higher than its parent. In which case, run:

```
void fixUp(index j) { // index j of table array
    while (parent(j) exists
        && table.at(j).value > table.at(parent(j)).value) {
        swap(table.at(j), table.at(parent(j)));
    }
    // ENS: table is a heap again, provided no other value changed.
```

If the value decreased, instead run:

```
void fixDown(index j) {
    while (j is not in the bottom &&
        table.at(j).value is not >= both children) {
        swap j with the larger child
    }
    // ENS: table is a heap again, if no other changes.
```

Both routines run in $O(\log n)$ time, and are just a re-conceptualization of the ideas for insert and pop:

```
void insert (I& newItem) { ②
    table.at (firstFree++) = newItem;
    fixUp (firstFree-1);
}
```

$O(\log n)$ time but often "lucky". Note $n = \text{firstFree}$.

```
I top() { // REQ: firstFree > 0
    return table.at(0);
}
```

```
void pop() { // Same REQ - test checks first,
    // throws exception if violated.
    table.at(0) = table.at(--firstFree);
    fixDown(0);
}
```

$O(\log n)$ time, really Θ since rarely "lucky".

The STL priority-queue class, part of $\langle \text{queue} \rangle$, provides the above methods, but not a public fixUp or fixDown that can be used with any index.

However, in $\langle \text{algorithm} \rangle$ the STL provides `void make_heap (RA iterator first, RA iterator last, COMP)` which executes the following loop when $\left\{ \begin{array}{l} \text{first} = 0 = \text{table.begin} \\ \text{last} = \text{firstFree} \text{ as iterat} \end{array} \right.$