

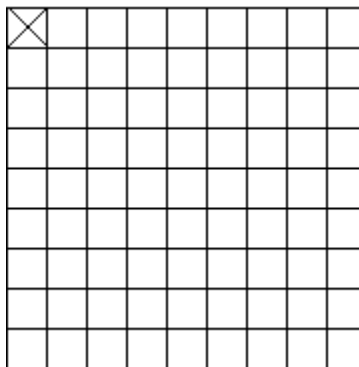
### Final Exam

Name \_\_\_\_\_

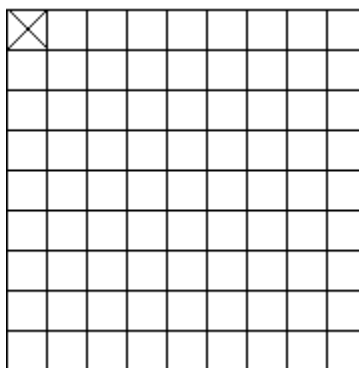
*Instructions: Write your name above and on the top of the second page. Do not remove the staple. Write answers here or in the bluebook provided as directed. This exam will be collected along with the blue book. 75 minutes closed book/notes no electronic devices permitted.*

1. Consider the blob  $X$  consisting of 80 object pixels arranged in a  $9 \times 9$  square:  $X = \{(0,0), \dots, (8,8)\}$ , where the middle pixel of this square, the pixel at  $(4,4)$ , is a background pixel.

(a) Find  $S_8(X)$ , the maximum ball skeleton of  $X$  using 8-connected distance measure. Show your answer by darkening each skeleton pixel in  $S_8(X)$  on the graph below. Explain your reasoning in the bluebook.



(b) Find  $S_4(X)$ , the maximum ball skeleton using the 4-connected distance measure. Show your answer by darkening each pixel in  $S_4(X)$  on the graph below. Explain your reasoning in the bluebook.



Name \_\_\_\_\_

2. The discrimination boundaries for a three-class decision problem over a two-dimensional feature space of vectors  $\mathbf{x}$  are shown below. They intersect at  $\mathbf{x} = (1,1)$ .

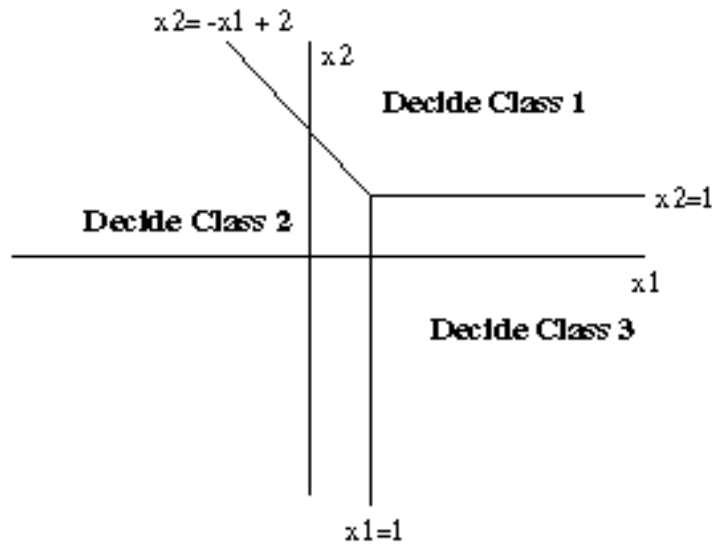


Figure 2

(a) Specify the  $(x_1, x_2)$  coordinates of 3 training atoms so that the minimum distance classifier trained using just this training data set agrees with the figure above.

(b) Is the set of 3 training data answering (a) above unique? If not, specify all sets of 3 training data which solve (a) above.

(c) Could Fig 2 be consistent with a Gaussian minimum-error classifier? If yes, specify mean vectors and covariance matrices  $\{\mu_i, \Sigma_i, i=1..3\}$ , also prior probabilities  $\{\pi_i, i=1..3\}$ , which make them consistent. If no, explain why not.

3. In a certain image we have found  $n \geq 3$  objects  $R_1 \dots R_n$ . We see that  $R_1$  is blue,  $R_2$  is green,  $R_3$  is yellow and that  $R_i$  is adjacent to  $R_{i+1}$  for  $i=1..n-1$ . We wish to classify these objects using label set  $\{O_1, \dots, O_m\}$ . The rules are that only  $O_1$  can be blue, and  $O_i$  and  $O_{i+1}$  must be adjacent for  $i=1..m-1$ . Now in the relaxation algorithm for constraint propagation we may check objects in any fixed order. Show that if we check objects in the order  $R_1$  to  $R_n$  the algorithm converges much faster than if we check in the reverse order,  $R_n$  to  $R_1$ . Specify all consistent label sets, and the number of iterations to convergence in each case.