### Lecture 22

CSE 331 Oct 15, 2014

## Graded Quiz 1

#### Will hand them out at the FND of the lecture



stop following



### Actions \*

#### Graded Quiz 1

Quiz 1 has been graded and your scores have been uploaded to UBLeams. I'm hoping to hand out the quizzes in class tomorrow (if not in the worst-case they'll be available for pickup at the extra office hours tomorrow @232).

#### First the stats:

- Mean: 3.83
- · Median: 4.5
- Std Dev: 2.28

Now to the grading rubric. First the rubric that is applicable to both Q1a and Q1b on the quiz:

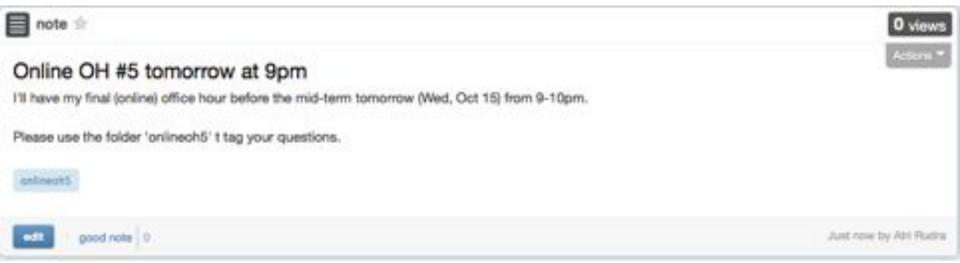
- 1. Two points for getting the T or F correct (which in this guiz was always true).
- 2. Three points for a correct justification.
- You get zero points if you state the T or F incorrectly (irrespective of what you stated in the justification part).

Note that we will also be using the same general rubric as above for the questions on the first mid-term.

Now for some more specific guidelines/mistakes for the justification parts:

- For Q 1a:
  - For a technically correct solution your algorithm should work for all graphs even if they are disconnected. However, you got full points for the
    justification part if your justification only worked for the case when G is connected.
  - If you mentioned DFS or BFS but rest of the stuff was wrong you got 1 out of 3.
  - 2. If you appeared an algorithm that one is O(a) time you got a people of 2 fairness the algorithm also has to absolute the an adjoint

## Online OH tonight @9pm



### Two definitions for schedules

Idle time

Max "gap" between two consecutively scheduled tasks

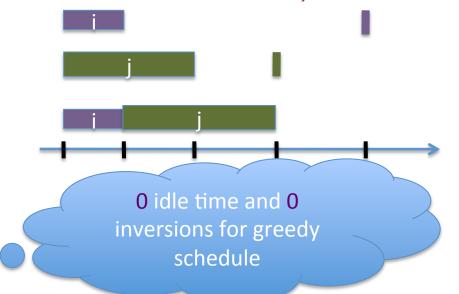


Inversion

f=f+t;

(i,j) is an inversion if i is scheduled before j but  $d_i > d_i$ 

f=1For every i in 1..n do
Schedule job i from  $s_i=f$  to  $f_i=f+t_i$ 



### Proof structure

Any two schedules with 0 idle time and 0 inversions have the same max lateness

Greedy schedule has 0 idle time and 0 inversions

There is an optimal schedule with 0 idle time and 0 inversions

# Today's agenda

"Exchange" argument to convert an optimal solution into a 0 inversion one

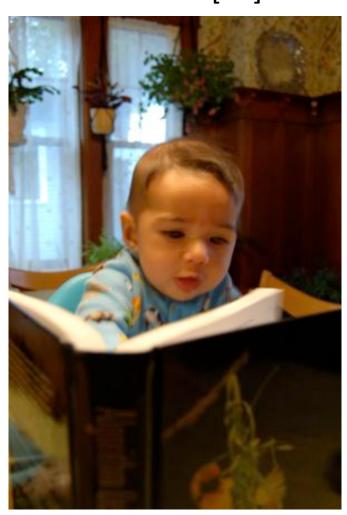
# **Rest of Today**

Buildings 60 Seconds When I'm walking, I worry a lot about the efficiency of my path. Building http://xkcd.com/85/

**Shortest Path Problem** 

# Reading Assignment

Sec 2.5 of [KT]

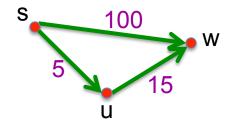


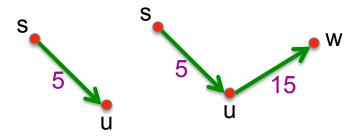
# Shortest Path problem

**Input:** *Directed* graph G=(V,E)

Edge lengths, l<sub>e</sub> for e in E

"start" vertex s in V



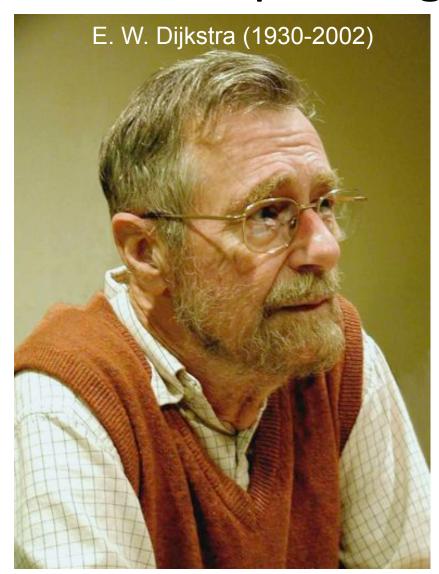


Output: All shortest paths from s to all nodes in V

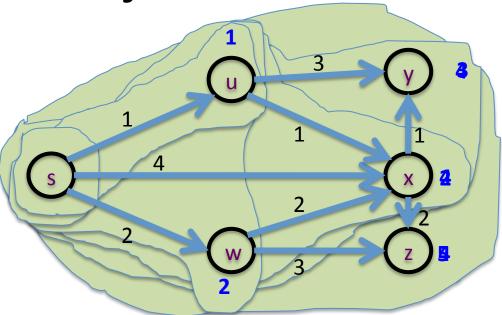
# Naïve Algorithm

 $\Omega(n!)$  time

# Dijkstra's shortest path algorithm



# Dijkstra's shortest path algorithm



Input: Directed G=(V,E),  $I_e \ge 0$ , s in V

$$R = \{s\}, d(s) = 0$$

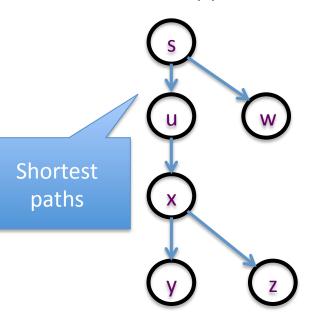
While there is a x not in R with (u,x) in E, u in R

Pick w that minimizes d' (w) Add w to R d(w) = d' (w)  $d'(w) = \min_{e=(u,w) \text{ in E, } u \text{ in R}} d(u) + I_e$ 

$$d(s) = 0$$
  $d(u) = 1$ 

$$d(w) = 2$$
  $d(x) = 2$ 

$$d(y) = 3$$
  $d(z) = 4$ 



## Couple of remarks

The Dijkstra's algo does not explicitly compute the shortest paths

Can maintain "shortest path tree" separately

Dijkstra's algorithm does not work with negative weights

Left as an exercise