Plagiarism will earn you an F in the course and a recommendation of expulsion from the university.

- 1. $T \wedge F =$
 - a. T
 - b. F
- 2. T V F =
 - c. F
 - d. T
- 3. Which of the following are predicates? Choose all that are correct.
 - a. x is odd.
 - b. 22 is a prime number.
 - c. $\frac{1}{1+x} < 1$.
 - d. $16 = x^2$.
 - e. There are 15 questions on this exam.
- 4. $\neg p \lor \neg q \equiv \neg (p \land q)$
 - a. True
 - b. False
- 5. $p \land q \equiv \neg (p \land \neg q)$
 - c. True
 - d. False
- 6. *A*={1,5,2,3}, *B*={1,2,5,3}
 - a. A=B
 - b. *A≠B*
- 7. *A*={1,2,3,4}, *B*={1,2,3,4,5}. Choose all that are correct.
 - a. $A \subset B$
 - b. $B \subset A$
 - c. $A \subseteq B$
 - d. $B \subseteq A$
 - e. *A* ⊈ *B*
- 8. *A*={1,2,3,4,5,6}, *B*={1,2,3,4,5}. Choose all that are correct.
 - a. $A \subset B$
 - b. $B \subset A$
 - c. $A \subseteq B$
 - d. $B \subseteq A$
 - e. *A* ⊈ *B*

- 9. *A*={1,2,3,4}, *B*={1,2,3,4,5}. Choose all that are correct.
 - a. $A \cap B = \{2\}$
 - b. $A \cap B = \{2,3\}$
 - c. $A \cap B = \{1, 2, 3, 4, 5\}$
 - d. $A \cap B = \{5\}$
 - e. $A \cap B = \{1, 2, 3, 4\}$

10. *A*={1,2,3,4}, *B*={1,2,3,4,5}. Choose all that are correct.

- a. $A \cup B = \{2\}$
- b. $A \cup B = \{2,3\}$
- c. $A \cup B = \{1, 2, 3, 4, 5\}$
- d. $A \cup B = \{5\}$
- e. $A \cup B = \{1, 2, 3, 4\}$
- 11. Let $c(x) = x^3$, where x is a real value. Choose all that are correct.
 - a. *c* is neither one-to-one nor onto.
 - b. *c* is one-to-one but not onto.
 - c. *c* is onto but not one-to-one.
 - d. *c* is both one-to-one and onto.
- 12. Choose all that are correct.
 - a. [10.9] = 10
 - b. [10.9] = 10
 - c. [10.1] = 10
 - d. [9.9] = 10
 - e. [9.1] = 10

13. $(A \cup B) \cup C = A \cup (B \cup C)$ is an example of which law.

- a. De Morgan's Law
- b. Law of Diminishing Returns
- c. Associative Law
- d. Commutative Law
- e. Murphy's Law

14. $\sum_{i=1}^{n} i =$

a.
$$n^2$$

b. $\frac{n(n+1)}{2}$
c. $\frac{(n-1)(n+1)}{2}$
d. n^3

e. Θ(*n*)

- 15. Let $X = \{u, v, w, y\}$. Define a function $g: X \to X$ to be $g = \{(u, v), (v, w), (w, y), (y, u)\}$. What is $g^{-1}(x)$? Choose all that apply.
 - a. {(*u*,*w*)}
 - b. $\{(y,u),(w,y),(v,w),(u,v)\}$
 - c. {(*w*,*u*)}
 - d. $\{(v,u),(w,v),(y,u),(w,y)\}$
 - e. None of the above

16.
$$\sum_{j=0}^{n} 2^{j}$$
=

- a. $2^{j} + \sum_{j=0}^{n-1} 2^{j}$
- b. $2^{n-1} + \sum_{j=0}^{n-1} 2^j$
- c. $2^n + \sum_{j=0}^{n-1} 2^j$
- d. $2^n + \sum_{j=0}^n 2^j$
- e. $\sum_{j=0}^{n/4} 4^j$
- 17. Given an ordered array of *n* items on a sequential computer (*i.e.*, a RAM), what is the worst-case (*i.e.*, longest) running time of Binary Search?
 - a. Θ(*n* log *n*)
 - b. Θ(*n*)
 - c. Θ(log n)
 - d. Θ(*n*²)
- 18. Given a list of *n* items, arbitrarily ordered on a sequential computer. Choose all that correctly describe the running time of (an efficient implementation of) MergeSort.
 - a. $\Theta(n \log n)$
 - b. Ω(*n*)
 - c. Θ(log *n*)
 - d. *O*(*n*²)
 - e. MergeSort has the same behavior, in terms of running time, as QuickSort.
- 19. Given a PRAM with *n* processors and *n* data initially distributed arbitrarily in the first *n* locations of the shared memory, the minimum value of these n items can be determined by using which technique.
 - a. Massively Exploding
 - b. Massively Imploding
 - c. Recursive Doubling
 - d. Recursive Halving
- 20. Suppose you are given a linear array of size *n* with *n* pieces of data initially distributed one per processor in an arbitrary fashion. Choose all that apply.
 - a. The minimum value requires $\Omega(n)$ time to be determined.
 - b. The minimum value can be determined in $\Theta(\log n)$ time.
 - c. The minimum value can be determine in $\Theta(n)$ time, which is asymptotically optimal for this architecture.
 - d. The minimum value is 1.
 - e. None of the above.

Extra Credit

- 21. Dr. Miller is a member of which Pop/Rock Band?
 - a. The False Implications
 - b. Florence and the Fender Precisions
 - c. Theorem and Lemmas
 - d. Escher's Enigma
 - e. Prof. Miller is not in a Pop/Rock Band.
- 22. What is the name of the software created by Dr. Miller's research group in molecular structure determination?
 - f. Prestige-Worldwide
 - g. Snoop-a-Loop
 - h. Shake-and-Bake
 - i. All-Along-The-Watchtower
 - j. None of the above. These are all phrases used by Will Farrell and have nothing to do with Dr. Miller's research.