The Story Next To the Story Behind the Results

"Pip" Buff Georgia Unitech

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- Can we modify the proof to work for criteria 2-4?