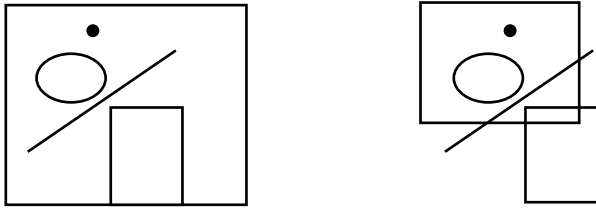


2D Graphics Primitives III

Clipping



Example: user change in window size and Expose event

Redraw entire image?

Redraw clipped image

Specifications of entire scene as lines, circles etc (OpenGL calls)

Scan convert entire scene into a pixmap

Copy portion of pixmap as specified by clipping rectangle

Versus

Specification of entire scene as above

Scan convert entire scene, but write only visible pixels

(Scissoring)

Versus

Specifications of entire scene as above

Specifications of clipped scene

Scan convert from clipped specifications

First is easy, but wastes time and space

Second may be quite efficient if done in microcode or hardware

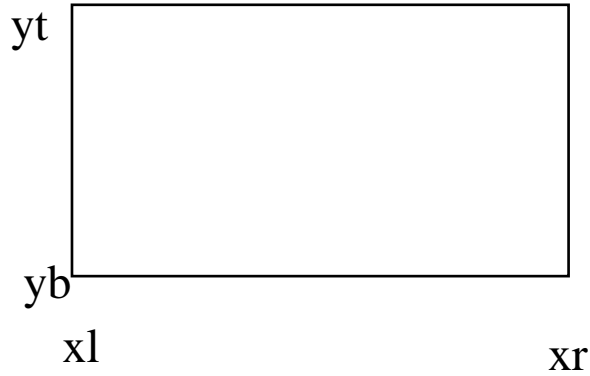
Generalizes to arbitrary shape clip regions

Third is often best for points, lines, polygons (simple algorithms)

Define Clip Rectangle (Region)

Start with rectangular clip region (clip-box)

defined by x_l , x_r , y_t , y_b

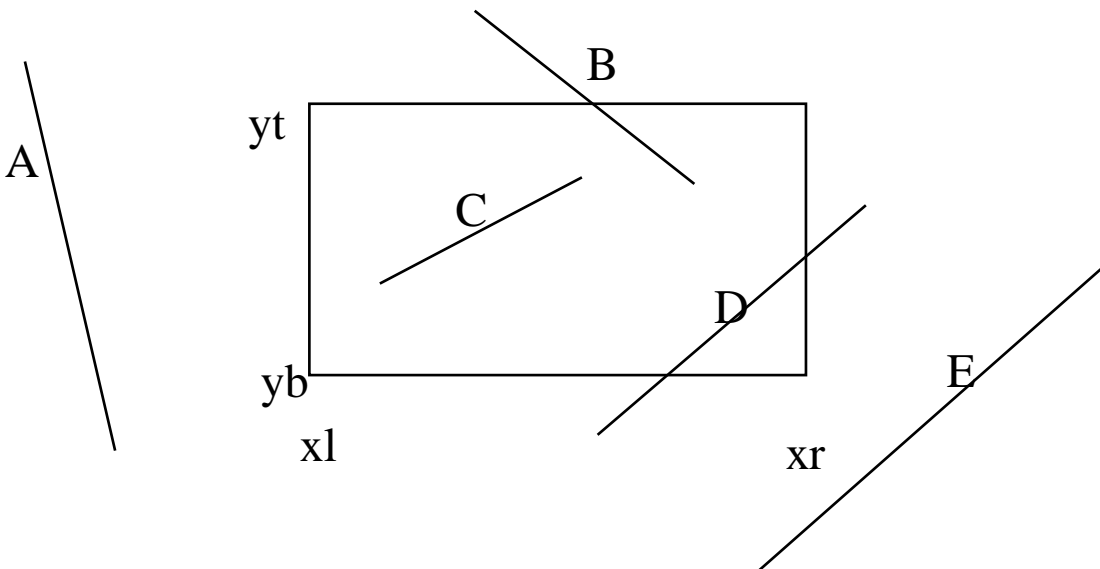


Clipping Points

How determine if point should be displayed?

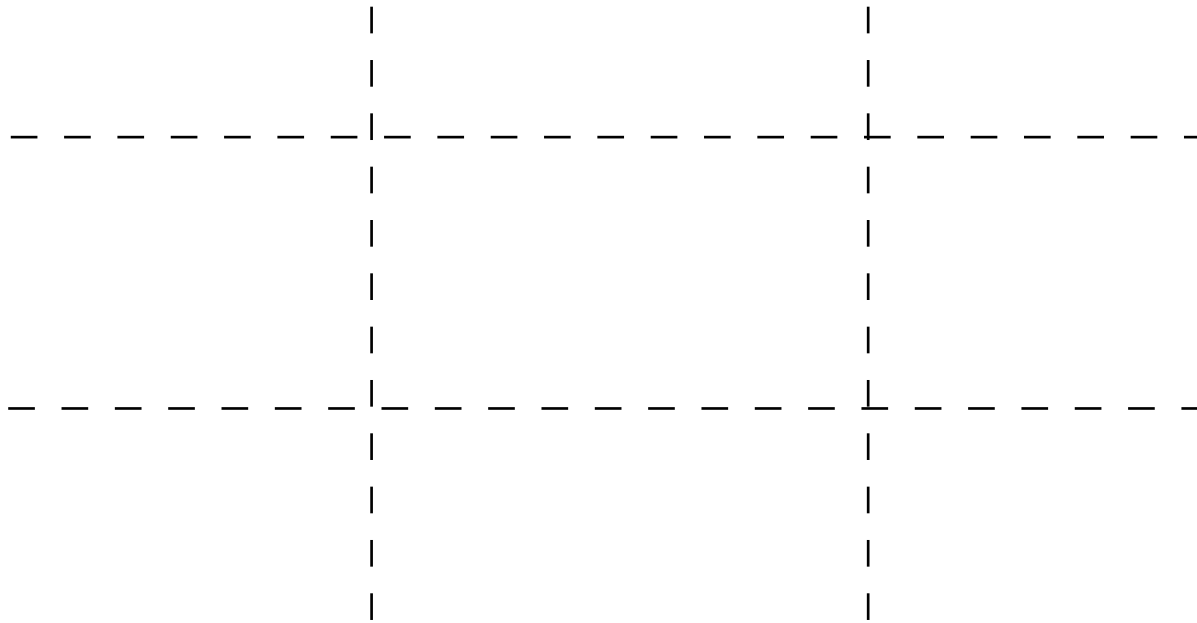
Clipping Lines

More difficult



Which lines easy to clip?

Cohen-Sutherland Line Clipping Algorithm



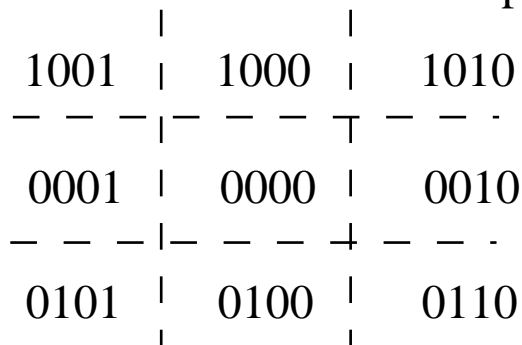
Based on idea that some lines are trivially accepted (entire line drawn)
 others trivially rejected (none of line drawn)
 others more difficult (maybe clip some, maybe draw nothing)

Look at nine regions of space as divided by the clip-box

Assign 4 bit region code to each region:

b4 b3 b2 b1

- b1 = 1 if point is to the left of the left boundary
- b2 = 1 if point is to the right of the right boundary
- b3 = 1 if point is below bottom boundary
- b4 = 1 if point is above top boundary

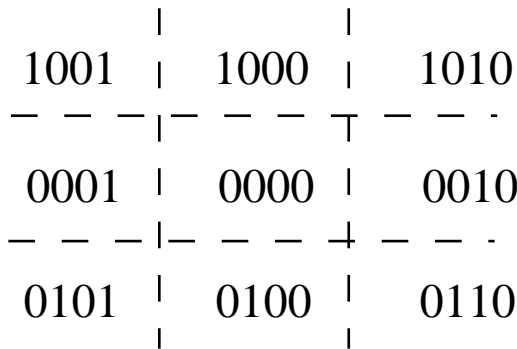


Find region code of each end of line
 (C1, C2)

Use to accept or reject line

eg if both ends are 0000?

what else is easy case?



Look at logical operations on the region codes (AND, OR)

- A) If $C1 \text{ OR } C2 = 0000$, then trivially accept line
- B) How trivially reject a line that has both points above top?
 $C1 \text{ AND } C2 = 1xxx$

How trivially reject a line below, to right and to left?
 $C1 \text{ AND } C2 = ?$
 $C1 \text{ AND } C2 = ?$
 $C1 \text{ AND } C2 = ?$

How generalize these four cases?
 $C1 \text{ AND } C2$ not equal 0000

- C) Rest are difficult
 $C1 \text{ AND } C2 = 0000$

Cohen-Sutherland Algorithm

Start with input list of lines (endpoints)

M: While input list is not empty

Find Region codes ($C1$ and $C2$) for line

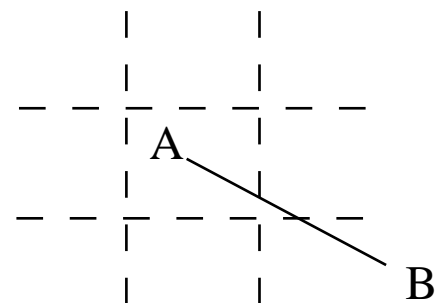
Remove line from input list

If $C1 \text{ OR } C2 = 0000$, then add line to output list

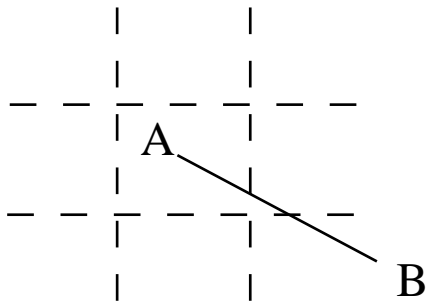
Else if $C1 \text{ AND } C2 = 0000$, find intersection of line with an edge (top, bottom, left, right order)

Add intersection point and interior point to input list

End

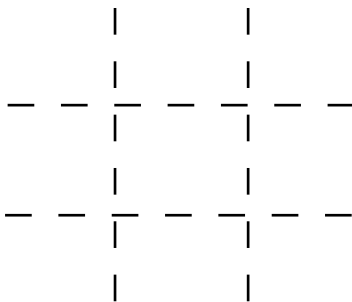


Given the order of testing for intersections, what is a worst case input line for Cohen-Sutherland algorithm?



This required two clips
 First required two tests
 Second required four tests

Can a line require 4 clips? (How many regions can a line pass through?)



If four clips required,
 then how many tests on first clip?
 on second?
 on third?
 on fourth?

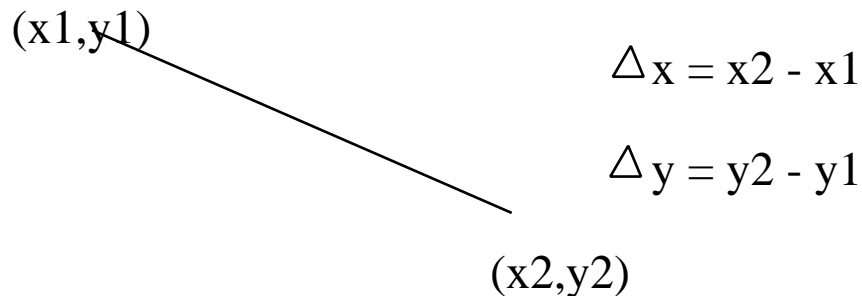
Cohen-Sutherland not the most efficient algorithm as it can end up doing needless clipping.
 Still used widely, since widely known

Cyrus-Beck Parametric Line Clipping Algorithm
 more efficient
 can clip against convex polygon clip region
 can clip in 3D as well as 2D

Liang-Barsky
 like above, but faster for upright rectangular 2D and 3D regions

Derivation of Liang-Barsky

Based on parametric representation of line



$$\begin{aligned} x &= x_1 + \Delta x u \\ y &= y_1 + \Delta y u \end{aligned} \quad 0 \leq u \leq 1$$

Write clipping equations in parametric form

$$x_L \leq x_1 + \Delta x u \leq x_R$$

$$y_b \leq y_1 + \Delta y u \leq y_t$$

Rewrite as four inequalities

$$u p_k \leq q_k, \text{ where } k = 1, 2, 3, 4$$

$$p_1 = -\Delta x \quad q_1 = x_1 - x_L$$

$$p_2 = \Delta x \quad q_2 = x_R - x_1$$

$$p_3 = -\Delta y \quad q_3 = y_1 - y_b$$

$$p_4 = \Delta y \quad q_4 = y_t - y_1$$

Each value of k corresponds to one boundary:

$k = 1$ corresponds to left boundary

$k = 2$ corresponds to the right boundary

$k = 3$?

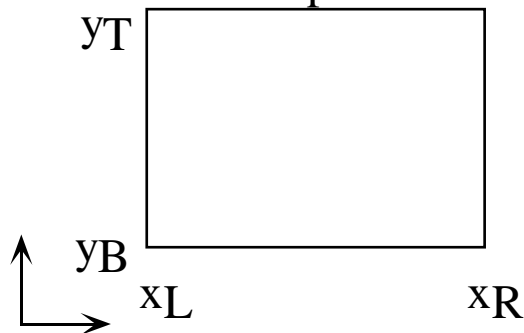
$k = 4$?

If line is parallel to the k th boundary, then

$p_k = ?$

The values of q_k indicate which side of the k th boundary

the start point is on



$$p_1 = \Delta x$$

$$q_1 = x_1 - x_L$$

$$p_2 = \Delta x$$

$$q_2 = x_R - x_1$$

$$p_3 = -\Delta y$$

$$q_3 = y_1 - y_B$$

$$p_4 = \Delta y$$

$$q_4 = y_T - y_1$$

if $q_k < 0$, then p_1 is outside k th boundary

$q_k \geq 0$, the p_1 is inside or on the k th boundary

if $p_k < 0$, then line goes from outside to inside the k th boundary

$p_k > 0$, then line goes from inside to outside the k th boundary

if $p_k = 0$, then the intersection of the line with the k th boundary is at

$$r_k = q_k / p_k$$

For each line we want to find u_1 and u_2 that lie in clip region

Liang-Barsky Algorithm

For each line segment

$u_1 = 0;$

$u_2 = 1;$ (We are starting with the original endpoints)

$k = 1;$

while still need to clip and $k \leq 4$

compute p_k and q_k

if $p_k = 0$ and $q_k < 0$, then reject line and stop clipping

else

if $p_k < 0$,

$u_1 = \text{maximum of } u_1 \text{ and } r_k$

else

$u_2 = \text{minimum of } u_2 \text{ and } r_k$

if $u_1 > u_2$

reject line and stop clipping

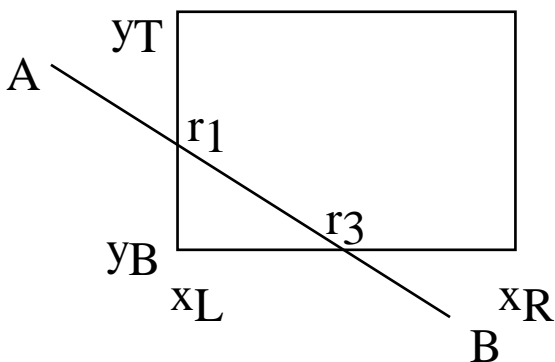
$k = k + 1;$

end

if line not rejected, u_1 and u_2 are end points of clipped line

end

Example:



Line AB

$$p_1 = \Delta x$$

$$q_1 = x_1 - x_L$$

$$p_2 = \Delta x$$

$$q_2 = x_R - x_1$$

$$p_3 = -\Delta y$$

$$q_3 = y_1 - y_B$$

$$p_4 = \Delta y$$

$$q_4 = y_T - y_1$$

$$u_1 = 0 \quad u_2 = 1$$

$$p_1 < 0$$

$$q_1 < 0$$

$$u_1 = r_1 \quad u_2 = 1$$

$$p_2 > 0$$

$$q_2 > 0$$

$$u_1 = r_1 \quad u_2 = 1$$

$$p_3 > 0$$

$$q_3 > 0$$

$$u_1 = r_1 \quad u_2 = r_3$$

$$p_4 < 0$$

$$q_4 > 0$$

$$u_1 = r_1 \quad u_2 = r_3$$

Liang-Barsky versus Cohen-Sutherland

Liang-Barsky computes fewer intersections for a line needing clipping

But doesn't have a trivial accept

If most lines can be trivially accepted or rejected,

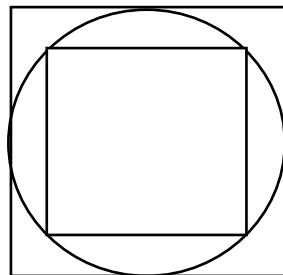
Use Cohen-Sutherland

else

Use Liang-Barsky

Clipping Circles

Can approximate with 2 rectangles for trivial accept and reject



Outer used for?

Inner used for?

Can make better approximations using polygons