# DILEMMA INFERENCE ON SNePS SEMANTIC NETWORK SYSTEM 

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## I. INTRODUCTION

This paper presents a package of LISP functions collectively called DILEMMA defined within the frame of MULTI IMcKay \& Shapiro (l980)], adding an extra bit to the existing capability of inference process possessed by SNePS semantic network processing system [Shapiro (1979a)].

Current inference mechanisms implemented on virtulally any semantic network systems are driven by essentially two basic operations: matching and data extension. Matching operation is to discover instances out of the database which will prove or disprove the queried theorem, while data extension operation is to expand the database through legitimate applications of inference rules upon the data available at the given moment in order to feed the matching operation with more data. We can thus view that inferencing is a series of computations in which these two basic operations are taking place repeatedly until either the theorem is proved or disproved or no more data extension is possible with the theorem yet undecided when the available data is exhausted.

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So far, a disjunctively asserted data items like
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(1) $P$ V $Q$
are regarded useless as data items in the database even if $P$ and $Q$ are individually a molecular constant. For instance, when one knows that "Tom is either a first-year graduate student or a senior undergraduate student of this department.", the current situation is such that that knowledge is not usable for answering such a question like "Is Tom a student of this department?".

The goal of this research is to add an extra set of control mechanisms to the present SNePS inference system so that it can now utilize such disjunctively asserted data as data item, not only as a rule if such data shows a possiblity of proving or disproving the queried theorem in one way or another. This technic of inference, which is traditionally called "dilemma inference", shows itself, in fact, not so rare in an actual human reasoning.

This paper has two folds. The first section is devoted to an examination of the anatomy of dilemma inference in terms of formal logic, and the latter section presents the new package as a program object describing its major components with some discussions on a few technical issues related to this implementation.
II. THE LOGICAL ASPECT OF DILEMMA INFERENCE

It looks like to me that the intrinsic mechanism of inference processes implemented on virtually all systems

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including SNePS is the so-called "disjunctive syllogism" which is
depicted by (2):
(2) # P v Q.
    # ~P.
    +Q.
where the meta-symbols have the following interpretations:
    # X.: "It is asserted that X is logically valid.";
    + X.: "It is derivable that X is logically valid.";
    . : (indicates the range of the last meta-symbol
                        # or +);
```

$\qquad$

``` : (indicates whatever above this is in database).
If we introduce another literal \(P^{\prime}\) which is logically complementary to \(P\left(i . e ., P^{\prime}=\sim P\right)\), then (2) can be rewritten into (3):
(3) \#~F'V Q.
\[
\text { \# } P^{\prime} \text {. }
\]
\[
+Q
\]
which is the canonical notation to express both syllogisms of modus ponens and modus tollens which are each conventionally represented by (4) and (5), respectively.
(4) \# \(P^{\prime}=>\quad 0\).
```

$$
\text { \# } P^{\prime} \text {. }
$$

$$
+Q .
$$

(5) $\quad P^{\prime} \Rightarrow 0$.
$\# \sim Q$.

$$
+\sim P^{\prime} \quad(=P)
$$

But, the constraint that the number of the terms appearing in the major premise has to be two seems uselessly too strong. And similarly, the number of expressions in the minor premise does not have to be one either (here, I will exclusively mean by "terms" the top-level disjuncts within a disjunctive proposition, and by "expressions" the top-level conjuncts within a conjunctive proposition). Thus, a more generalized disjunctive syllogism is formalized as (6):
(6)

$$
\left.\begin{array}{llllll}
\# P_{1} & v & P_{2} v & \ldots & v & P_{n} \\
\# & \sim Q_{1} & \wedge & \sim Q_{2} & \wedge & \ldots
\end{array}\right) \sim \sim Q_{m} .
$$

$$
+R_{1} v R_{2} v \ldots \vee R_{n-m}
$$

where $Q_{i}$ e $A=\left\{P_{j}\right\}$,
$R_{k} \in A-\left\{Q_{i}\right\}$,
$m<n, \quad 1=<i=<m, \quad 1=<j=<n, 1=<k=<n-m$.

It is immediatly recognized that representing (6) in an implication format will be extremely cumbersome and wasty because there exist roughly $2^{\text {n }}$ number of different ways of grouping the terms appearing in the major premise into two partitioned sets
(one for the antecedent and another for the consequent), and every different partition will require each unique implication of its own. A bi-directional use of one implication can reduce that explosive number by one half only.

We now clearly see that the operation of data extension in a deductive inference process conventionally implemented on most systems using the material implication is a proper subset of this generalized disjunctive syllogism. The underlying idea of a deductive inference is that, if we design a database in a certain way abiding some constraint(s), then, when a part of the data turns out to have a certain logical value, may we possibly predict the logical value of some part of the rest of the data. Two different constraints very likely useful in constructing a database come to our mind. One constraint is to keep the overall logical value of the whole database being inconsistant, while another is to keep it being valid. A system which maintains the overall logical value to be valid is called a "truth-maintenance system" (TMS). And a system which maintains the overall logical value to be inconsistant may be analogously called an "inconsistant-maintenance system" (IMS). A TMS system will crash with even a single invalid expression connected by a logical AND on the top level. Similarly, an IMS system will crash with even a single consistant term connected by a logical OR on the top level. Therefore, if the whole database is going to be decomposed into a number of independent partitions connected all together by an appropriate logical connective on the top level (AND for a TMS system and OR for an IMS system), then it becomes essential to assure that the logical value of each partitioned
data component is also valid for a TMS system and inconsistant for an IMS system. If a TMS system consisted of a top-level OR, then any one valid component will make the rest of the whole database uninteresting, and thus we can no longer find independence relation among the top-level components. A similar claim is also applicable to an IMS system as to top-level AND connection. It becomes thus clear why an appropriate top-level logical connective to integrate the whole database must be chosen so as to make the database non-trivially useful depending on the orientation of the system's truth-value maintenance. Thus, it becomes clear that the top-level data structure of a TMS system is a conjunction of disjunctions, while the top-level data structure of an IMS would be, if it be ever tried, a disjunction of conjunctions. And, we further see that, in a TMS system, disjunctive syllogism is the fundamental tool for inference.

Then, we may easily imagine another type of tool for inference, namely, conjunctive syllogism on an IMS system which is depicted by (7).
(7)

$$
\left.\begin{array}{lllllll}
: \# & P_{1} & \wedge & P_{2} & \ldots & \ldots & P_{n} \\
: \# & \sim Q_{1} & v & \sim Q_{2} & v & \ldots & v
\end{array}\right) \sim Q_{m} .
$$

$$
i+R_{1} \wedge R_{2} \wedge \ldots \sim R_{n-m}
$$

Where the meta-symbols have the following meanings:
:\# X.: "It is asserted that $X$ is inconsistant.";
i+ X.: "It is derivable that $X$ is inconsistant.";
and all the others rest the same as in (6).

However, if we pretend that "consistant" and "valid" are equivalent, and "inconsistant" and "invalid" are also equivalent (as is in a monotonic logic), then, by replacing each of the meta-symbols i\# and :+ by a \# and +, respectively, together with a negation associated to every of them, we can equivalently transform (7) into (8):
(8)

$$
+\sim\left[R_{1} \wedge R_{2} \wedge \ldots \wedge R_{n-m}\right]
$$

where all the conditions rest the same as in (7).

Using de Morgan's law, (8) is rewritten into (9):
(9)

$$
+\sim \sim R_{1} \vee \sim R_{2} \vee \ldots v \sim R_{n-m} .
$$

where all the conditions rest the same as in ( 8 ).

If we introduce new atoms, which are each a logically complement of a negated atom in the set, and are each named by adding a prime (diacritic) to the name of its complementary original atom, then we can rewrite all the propositions using these newly introduced atoms only, getting (10) from (9).

$$
+R_{1}^{\prime} v^{\prime} R_{2} v \ldots v R_{n-m} .
$$

$$
\begin{align*}
& \text { \# } P_{1}^{\prime} v P^{\prime}{ }_{2} v \ldots . . . v P_{n}^{\prime} . \tag{10}
\end{align*}
$$

$$
\begin{aligned}
& \# \quad \sim P_{1} \quad v \quad \sim P_{2} v \ldots v \quad \sim P_{n} . \\
& \text { \# } Q_{1} \wedge Q_{2} \wedge \ldots \wedge Q_{m}
\end{aligned}
$$

$$
\begin{aligned}
& \text { \# } \sim 1 \mathrm{P}_{1} \wedge \mathrm{P}_{2} \wedge \ldots{ }^{\wedge} \ldots \mathrm{P}_{\mathrm{n}} \text {. } \text {. } \\
& \text { \# } \sim\left[\begin{array}{lllllll} 
& \sim Q_{1} & v & \sim Q_{2} & v & \ldots & v
\end{array} \sim Q_{m}\right] .
\end{aligned}
$$

where, if the complementary relation
is appropriately considered, all the conditions rest analogously the same as in (9).

We see that (10) is syntactically identical to (6), which is a formalization of a disjunctive syllogism on a TMS system. Hence, we now realize that disjunctive syllogisms and conjunctive syllogisms are isomorphic to one another in a monotonic logic. To put this in another way, the duality of a logical model enables us to construct an equally healthy model (as much healthy as the original) by exclusively exchanging all conjunctions with disjunctions and vice versa, all assertions with negations and vice versa, and all interpretation of "valid" with "inconsistant" and vice versa [Kleene (1967:22)]. Thus so far, we have shown that disjunctive syllogism may be adopted as a cannonical notation for all inference mechanism, and that any significant development of inference technic will probably be captured by this cannonical representation inference mechanism.

But, I would like to point out here that it is not our original purpose just to claim that the disjunctive syllogism-like notation can be a cannonical representation of any inference mechanisms. We rather want to look into the behavior of conventional inference mechanism with the aid of this cannonical representation, and attempt to find out any possible factors that we may be able to improve.

I think there are at least two heels of Achiles embedded in most of the currently running inference systems. One is that it is always assumed that the negation of "valid" is necessarily
equivalent to "inconsistant", and vice versa, so that a system hardly knows how it can be modest by saying "Sorry, I don't really know. I can't really say anything.". Thus, one possible revolt can be not granting the monotonicity of the interpretation of a system's logical value. How to construct a system that computes deductive inferences on a non-monotonic logic appears to be an interesting worthy problem.

But, granting the monotonicity of logic, and thus pretending that the frame of disjunctive syllogism is the basic tool for all deductive inferences, another taboo which was not challenged by current systems appears to be the assumption that a minor premise is necessarily a single term. What kind of inference can be performed if a minor premise turns out to be a disjunction of syllogisms, the conclusion of a unit syllogism is supposed to be a disjunction of more than one term ?

Let $D_{1}$ and $D_{2}$ be two independently valid disjunctive syllogisms like the one whose schemata was defined in (6), and $M(D), m(D)$, and $C(D)$ respectively refer to major premise, minor premise, and conclusion of a disjunctive syllogism D. And let us define an operation * that applies on two disjunctive syllogisms such that $D_{1} * D_{2}$ represents a new disjunctive syllogism which is a composition of $D_{1}$ and $D_{2}$ as described in (11).
(I1)

$$
\begin{array}{rllll}
D_{1} * D_{2} & \Leftrightarrow & M\left(D_{1}\right) & \wedge & M\left(D_{2}\right) \\
& \# & m\left(D_{1}\right) & v & m\left(D_{2}\right)
\end{array}
$$

$$
+C\left(D_{1}\right) \quad v \quad C\left(D_{2}\right)
$$

A careful calculation will prove that $D_{1} * D_{2}$ is also valid if $D_{1}$ and $D_{2}$ are valid individually. Further more, it can be also shown that * operation is associative and commutative and can be applied abitrarily many times whose result is eventually given as shown in (12).
(12)

$$
\begin{array}{llllllll}
\# & X_{1} & \wedge & X_{2} & \wedge & \ldots & \wedge & X_{m} \\
\# & y_{1} & v & y_{2} & v & \ldots & v & y_{m} .
\end{array}
$$

$$
+\mathrm{Z}_{1} \vee \mathrm{Z}_{2} \vee \cdots \quad \ldots \quad v \quad \mathrm{Z}_{\mathrm{m}} \text {. }
$$

where

$$
X_{i}=P_{i 1} v P_{i 2} v \ldots v P_{i m\langle i\rangle},
$$

$$
Y_{j}=\sim P_{j 1} \wedge \sim P_{j 2} \wedge \ldots \wedge \sim P_{j n\langle j\rangle},
$$

$$
Z_{j}=Q_{j 1} v Q_{j 2} v \ldots v Q_{j(m\langle j\rangle-n\langle j\rangle)},
$$

where $Q_{j t} e A_{j}$,
$t=m\langle j\rangle-n\langle j\rangle$,
$A_{j}=\left\{P_{j 1}, P_{j 2}, \ldots, P_{j m\langle j\rangle}\right\}-B_{j}$,
$B_{j}=\left\langle P_{j k}\right\}$,
$1=\langle k=\langle n\langle j\rangle$,
$1=\langle i, j=\langle m, \quad n\langle j\rangle=\langle m\langle j\rangle$,

A simple example of this expanded disjunctive syllogism is given by (13).

```
(13) * ( \(\left.P_{11} \vee P_{13}\right) \quad \wedge \quad\left(P_{21} \vee P_{22}\right)\).
\[
\# \quad \sim P_{11} \quad v \quad \sim P_{21} .
\]
```

$$
+P_{12} \quad v \quad P_{22} .
$$

Here in this example, we can easyily see that the major premise has two expressions and both the minor premise and the conclusion also have two terms, and that the terms there are each one-to-one
associated with each expression in the major premise.

An eyeball examination tells us that (13) is nothing else but the canonical notation of a simplex dilemma as shown by (14).
(14) * $\left(P_{11}^{\prime} \Rightarrow P_{12}\right) \sim\left(P_{21}^{\prime} \Rightarrow P_{22}\right)$.

$$
\text { * } P_{11}^{\prime} V P_{21}^{\prime}
$$

$$
+P_{12} \quad \vee P_{22}
$$

where $P_{i j}^{\prime}=\sim P_{i j}$.

Since old Greek sophists paid them a great deal of attention, dilemmas (di- for two and lemma for assumption or proposition have been long regarded as one of the most powerful tools for a debate and has attracted much of logicians' interest. To describe it verbally, the format of a dilemma is that the major premise is a conjunction of arbitrary number of implications, and the minor premise is either a disjunction of every antecedent or a disjunction of the negation of every consequent. Of course, the conclusion is either a disjunction of every consequent or a disjunction of the negation of every antecedent. Traditionally, the terms listed in the monor premise were called "horns" of the dilemma, and completing an exhaustive list of all possible horns were known as an ultimate technic of developing strong arguments using a dilemma. Two well-known standard technics of attacking a dilemma argument were known to be either to seek any propositions not listed in the major premise that may produce a couter-argument unfavorable to the dilemma argument (-- "to take horns"), or to seek some missing


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horns that may provide a counter-argument unfavorable to the dilemma argument (-- to evade between horns). Depending on whether a dilemma is run in modus ponens or nodus tollens, it was called "constructive" or "destructive", respectively. And further, whether the conclusion of dilemma was merged into one single term or not, the distinction between a "simplex" and a "complex" dilemma was also made.

To my knowledge, no system has attempted to implement this most general schemata of disjunctive syllogism which seems to me to be able to accomodate any kind of inference mechanisms including simple disjunctive syllogisms.


## III. IMPLEMENTATION OF DILEMMA INFERENCE

## 1. Motivation

We pointed out already that dilemma is a special type of inference mechanism which may be viewed as a set of parallelly processed simplex disjunctive syllogisms among which a special inter-relationship * operation holds as defined. In most situation, however, we would not really appreciate this too complex process just in order to obtain a set of disjunctive conclusion with which one can hardly do anything. But, if in some situation, the conclusion happens to be merged into one single term (which is the case of a simplex dilemma), then we find that having the dilemma inference machanism available will sometimes enable a system to derive a conclusion which one would
normally want but could not get. Two examples of typical benefits we can get through this dilemma inference are shown by (15) and by (16).
(15)

```
# (\forallx)(Animal(x) => Breathe(x))
#(\forally)(plant(x) => Breathe(x))
# (\forallz)(Alive(z) => Animal(z) v Plant(z))
```

$+(\forall w)(A l i v e(w) \Rightarrow$ Breathe (w) $)$
(16)
\# On(block1, block2).

* On(block2, block3).
\# Red(blocki).
\# Red(block3).
* Red(block2) v Blue(block3).

```
+(3x3y)(Red(x)^ Blue(y) ^On(x,y)).
```

where all the predicates in (15) and (16) are dummy symbols for some appropriate n-ary predicates (But, readers are not discouraged to make a possible association for each of these with any tangible interpretation they may like to imagine).

The example (15) shows that dilemma inference can be used to derive new inference rules ("patterns" in a network term) which is not supprising since dilemma inference is a meta-mechanism which is ablout rule schematas. The example shown by (16), which is one of the famous problems in AI community known as "three-box problem" sheds another interesting point. The conclusion in the
process (16) asserts that there exist some $x$ and some $y$ such that the formula in the conclusion has an actual instanciation. Usually, a formula with unbound variable or a disjunctively asserted assertion is worthless for a final use. However, we notice that the conclusion drawn in (16) is already usable enough to answer a query that simply asks whether or not there exists such an instance not necessarily demanding to learn the exact binding situation. However, there may be someone who may wonder if (16), with a disjunctive assertion still in the conclusion, is within the frame of a simplex constructive dilemma which requires its conclusion to be a merged single term. We believe that it is so, but in one level higher order, though. To prove it, let us define $P$ and $E$ such that

$$
\begin{align*}
& P(x, y) \Leftrightarrow O n(x, y) \wedge \operatorname{Red}(x) \wedge \text { Blue }(y) \text {, and }  \tag{17}\\
& E(q) \Leftrightarrow(\exists x \exists y)(q(x, y)) .
\end{align*}
$$

Certainly, E(P) will have an interpretation that says "there is at least one instance of $P$, a binary predicate.". With this definition, we can then rewrite (16) into (18).
(18) * P(blockl, block2) $\Rightarrow E(P)$.
\# P(block2, block3) $\Rightarrow E(P)$.
\# P(blockl, block2) $V$ P(block2, block3).
$+$
$E(P)$.

Notice that (18) conforms precisely the schemata of simplex constructive dilemma, but where a predicate $P$ is used as an argument of a new higher order predicate $E$.

## 2. Solution on SNePS

First of all, it will be a good procedure to describe very briefly the present status and the nature of SNePS semantic network procesing system being maintained at the Department of Computer Science at State University of New York at Buffalo. SNePS can hold semantic information represented in the net as a set of associated network, and can perform backward inference for a specific theorem queried while a limited depth of forward inference may be also done. Inference mechanisms being used includes resource limited inference and ANDOR computation [Shapiro (1979b)] on top of the standard material implication. These various inference mechanisms are run in multi-processing mode in which a maximum data sharing becomes possible.

One of the conceivable ways of approaching to the implementation of dilemma inference to SNePS could be a utilization of already available inference mechanisms with a little addition of extra control. Among others, AND-IMPLICATION mechanism may appears to be very plausible. It proves a given theorem only when all the antecedents are proved. Considering that a dilemma inference proves a theorem only when the theorem is proved with every horn, we can realize that there is an AND-IMPLICATION's nature in a dilemma inference. From this, we can obviously derive a rule (19) which says:

$$
\begin{equation*}
(\mathrm{H} \Rightarrow T)=>\quad T \tag{19}
\end{equation*}
$$

where $H$ is a set of all horns, and $T$ is a queried theorem. This rule represented by (19) is a tautology mo matter what Thappens
to be. Thus, adding this rule to the database does not cause any protlem as far as the truth-maintaining tusiness is concerned, Due to this rule, then we may initiate ANG-IMFLICATION mechanism: and wait until this process returns an answer? If ANL-MMFLICATION proves $T$, then by the rule (17), we do prove $T$. Eut, a close examination shows us that this is not a solution by any means. Because the disjunctively asserted data will not be utilized by the AND-IMFLICATION process, the rule has no significance at all as far as dilemma inference is concerned. It is just like your saying that if you prove it then it is proved.

Discussing AND-OF tree problem solving techmic, Nilsson (1980) illustrated that the three-tox problem is a very peculiar kind of a graph-like AND tree protilem where there are two roots at both of which the control paths should communicate. Orie root is the node representing the given goal while another is the node that provides the disjunctive instance leading to a solution via "reasoning-by-cases" strategy, It is ari AND tree because every branch of the disjunctive instance must succeed in proving the theorem in order to prove the theorem, In an ordinary AND-DF tree protlem solving, the goal mode ereates descendent ANI or dR nodes, and lets them run to see who brings back which anwer. However, in this peculiar situation that he called the case of reasoning-by-cases strategy, an AND tree is freated from the node that represents the disjunctive assertion, and the goal node can make a decion when the AND tree created by someone else reports to him that every branch has been successfully terminated. Thus, he stated that the key to the solution of this strategy is somehow to make it fossible for the two critical nodes to
communicate. This matter could be resolved pretty easily on SNePS running on MULTI. When a top level inference mechanism finds a disfunctive assertion which seemingly has a potentiality of proving the theorem in a reasoning-by-cases fashion, the top level inference driver sets up a specialist who will take care of the dilemma inference case. Upon being set up, the specialist creates each case handler for every horn resolution, and instructs each of them to report to himself, and then waits until all horns sends him a message of success.

The real harder problem of a dilemma inference rather lies in the way how each of the horn attackers can resolves his own problem. Each horn attacker is of course expected to call for the help of inference specialist forming a daisy-chain recursion in order to solve his horn resolution problem with his particular horn assumption. In a data-sharing system like present SNePS running on MULTI, a horn assumption may not safely be added to the database as if it were real to everybody since it will mess up all other innocent processes sharing the data.

Thus, the way how the horn assumption is handled for each horn resolution seems to be the real core of the solution to dilemma inference (or reasoning-by-cases).

The solution which is adopted by this implimentation is to let the horn attacker reshape his own theorem derived from the original theorem that the dilemma process boss has been asked about. Each horn attacker is asked to prove the grand theoren with one's own horn assumption taken granted. A different assumption leaves a different subtheorem to be proved. For


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instance, if the horn assumption were the original theorem itself, then that particular horn attacker does not have to do anything. His duty is none from the very beginning. All he has to do is to report that with his horn assumption, the theorem is proved. Reshaping of theorem clearly does not affect the database, and makes a change onto the theorem ultimately to be proved, thus raising the possibility of the theorem's being proved.


## 3. Erogram description

On top of number of supporting lisp functions, this program package consists of four newly defined MULTI processes and two pre-existing processes slightly modified so that this package can be coupled to the present SNePS inference package. Each process is described as follows:

## INFER

This is a pre-existing process which cranks the main piston of inference machinary. This was modified so that it collects available and relevant horn sets for a given theorem to be proved. Dilemma inference is triggered only when the global switch <DILEMMA> is set to $T$, which is the default value at the top-most top level. If any horn sets are collected, INFER creates D-INFER and D-ANSCAT with the help of a lisp function <dilemma-infer>.

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receive disjunctive answers obtained throuhgh dilemma inference via a different process registor. The reason it does not use the normal message channel is in order not to cause the disjunctive answer to be permenantly built as other type of answers are. The deep reason why a disjunctive answer must not be permenantly built is that a dilemma inference cannot determine the number value for MAX arc. The routine assigns the maximum value for MAX for the sake of the largest generality, but certainly the system does not want it to serve as inference rules for any further inference.


D-INFER and D-ANSCAT

D-INFER creates appropriately many horn attackers ATTACK.HORN and one D-ANSCAT. ATTACK.HORN's are each given a horn to be disjunctively proved, and D-ANSCAT collects the answers coming from individual ATTAC.HORN's. When all horn aresuccessfully finished, D-ANSCAT send the anwer ldisjunctively bound binging set) to whoever ordered the dilemma inference work.

ATTACK.HORN AND HORN-ANSCAT

ATTACK.HORN reshapes the local theorem related to the horn assumption, and initiate INFER recursively to resolve the horn. In this embedded call to INFER, the switch <dilemma> is set to NIL such that too much costing dilemma inference may not be triggered within the embedded level. HORN-ANSCAT catches answers from ATTACK.HORN's clients and sends it to D-ANSCAT.

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## ?(INFUT DTLMA)

(INFER GATHER.HORNS WORTH-DIL? D-HORN? NO-FREEVAR? NON-NTLS ATOMOLECULE? DILEMMA-TNFER DILEMMA D-INFER ALL-HORNS? ATTACK.HORN HORN-TORN-CO INTOR N-CO SELECT. HORNS SORT.HORNE PACK-IN PUTTN-BASKET SET. PREG EQUISET HORNANSCAT D-ANSCAT RECORD. DANS DLLEM-RPT DRAFT.D-ANS TOPMOST-TOPINF DEDICE* D-5END)
?(INSYS MEMO)
(SNEPS FILE LOADED)
TOILEMMA
$T$
( (SNEPS)

## SNEPS

** (DESCRIBE (M1 M2 M3 M4 MS M6 M7 M8 M9 M10 M11))
(M1 (OBU (BLOCKZ)) (GUBJ (BLOCK1)) (REL (ON)))
(M2 (OBU (BLOCK3)) (SUBU (BLOCK2)) (REL (ON)))
(M3 (OBJ (BLOCK12)) (SUBJ (BLOCK11)) (REL (ON)))
(MA (COLOR (RED)) (P.OWN (BLOCK1)))
(M5 (COLOR (BLIE)) ( P . OWN (BLOCKO)))
(ME (COLOR (RED)) (P.OWN (BLOCK2)))
(M7 (COLOR (BLUE)) ( F : OWN (BLOCKZ)))
(M8 (ARG (M7 (COLOR (BLUE)) (P.OWN (BLOCK2)))
(ME (COLOR (RED)) (P.OHN (BLOCK2))))
(MAX (1))
(MIN (1)))
(M9 (COLOR (BLUE)) (F.OWN (BLOCK11)))
(M10 (COLOR (RED)) (P.OWN (BLOCK12)))
(M11)
( DUMFED)
627 MSECS
** (DEDUCE F.OWN BLOCI 2 COLOR $7 X$ )

FOR A OILEMMA INFERENCE,
WE KNOW
(H8 (ARG (M7 (COLOR (BLIUE)) (P.OWN (BLOCK2)))
(ME (COLOR (RED)) (P.OWN (BLOCK2))))
(mAX (1))
(MIN (1)))
HERE, WE INFER A DISULNCTIVE ANSWER
(T87 (ARG (T86 (COLOR (BLUE)) (P.OWN (BLOCK2))) (T85 (COLOR (RED)) (P.OWN (BLOCK2))))
(MIN (1))
(MAX (2)))

NIL
882 MEECS
** (DEDUCE MIN 3 MAX 3 ARG:

* (TBUTLD SUBJ \%X OBJ \%Y REL ON)
* (TBUILD P.OWN *X COLOR REO)
* (TBUTLD P.OWN *Y COLOR BLUE)))


## FOR A DILEMMA INFERENCE,

HE KNOW
(M8 (ARG (M7 (COLOR (BLUE)) (P.OWN (BLOCK2)))
(MO (COLOR (RED)) (P.OWN (BLOCK2))))
(MAX (1))
(MIN (1))

```
    A HORN TRIGGERS INFER TO PROUE T116
    HERE,WE INFER A DIEJUNCTTUE ANSWER
{T153
    (:SVAR (Q100 (:UAR (T))) (Q101 (:UAR (T))))
    (ARG
        (T152
            (ARG
                (TIS1 (REL (ON))
                        (OBJ (BLOCKZ))
                        (:SVAR (Q100 (:VAR (T))))
                            (SIBU (0100 (:UAR (T)))))
                (T150 (COLOR (RED)) (:SUAR (N100 (:VAR (T)))) (F.OWN (0100 (:VAR (T)
                )\))
                (T147 (COLOR (BLUE)) {P.OWN (BLOCK2))))
                (:SUAR (Q100 (:UAR (T))))
                (MAX (3))
                (MIN (3)))
        (T148
                (:SUAR (Q101 (:UAR (T))))
                \ARG
                (T147 (REL (ON))
                    (:SUAR (Q101 (:UAR (T))))
                    (OBU (Q101 (:VAR (T))))
                    (SUBJ (BLOCK2)))
                (T146 (COLOR (RED)) (F.OWN (BLOCN2)))
                (T145 (COLOR (BLUE)) (:SUAR (O101 (:UAR (T)))) (P.OWN (Q101 (:VAR (T
                ));))
            (mex (3))
            (MIN (3))))
    (MIN (1))
    (max (2)))
NIL
2259 MSECS
** (LISP)
END SNEPS
    ?(GRIND DLLMA XREF ALPHA 70)
```

                DILMA
                22 DECEMBER \(1781 \quad 2.52 .24\)
                CREATED: 14 DECEMBER 1981 21.31.24
                LAST MODIFIED: 22 DECEMBEF 17812.15 .28
                CHANGES MADE TO: DEDUCE: D-ANSCAT ATTACK.HORN
                                    ALL-HORNS?
    INFER


* [ALL-HORNE?] TESTS IF OR NOT EACH HORN INFERENCE HAS BEEN FINISHED
* WITH EUERY HORN IN THE HORN-SET EETNG MADE AS AN ASSIMPTION.
* THE ASGED GUERY IS DISJUNCTIVELY ANSWERED ONLY WHEN THE INFERENCE FOR EUERY
* HORN AS AN ASSUMPTION HOLDS.
* 

HYY -- 12/21/81

ALL-HORNS?
VALUE
(LAMBDA (REG NHORN) (AND (EQ (LENGTH REG) NHORN) (NON-NILE (MAPCAR REG CDR))))

PLIST
NIL

```
        ATOMOLECULE?
VALUE
(LAMBDA (NDE)
    (NON-NILS (MAPCAR (DOWNSET NDE)
                    (LAMBDA (ARGT)
                            (OR (NUMBERP (CDR ARGT)) (NULL (DOWNSET (CDR ARGT)))))))
)
PLIST
NIL
********************************************************************************
* PROCESS [ATTACK.HORN] TAKES CARE OF THE INFERENCE OF THE GIVEN CO WITH
* THE ASEUMPTION THAT THE HORN IS TRUE. THUS, THE NEN CO* TO BE PROUED
* IS "CO - HORN" WITH THE BINGING PROUIDED BY THE HORN ASSUMPTION.
#
                                    HYY - - 12/21/81
```

```
        ATTACK.HORN
VALUE
(LAmBDA (NAME: CLINK:% CQ: BNDG:)
    (COND ((NIILL CQ:) (SEND (LIST T) CLINK::))
        (T {PRIN3 & " A HORN TRIGGERS INFER TO PROVE " * CO:)
                {NEN-OLD-INFER CN: BNOG: CLINK:`)))
```

PLIST
(LREGS: (NAME: CLINE: CR: BNDG:))


* [LI-RNSCAT] PROCESS CATCHES THE ANSWERS FOR EUERY HORN INFERENCE, AND KEEPS
* CHECKING IF ALL HORNS PRODUCE EACH A DISJINCTIUE ANSWER. IF SO, THEN THIS
* PROCESS REPORTS THE ASNWER TO CLTNK: SNHORN: A REMEMEMBERS THE NUMBER OF
* HORNS, SREG: KEEPS ALL THE ANSHERS, SFLG: SIGNAL GETS OFF AFTER ONE SET
* OF ANSNER IS SENT TO CLINK:. BUT ALL THE ANSHER ARE CONTINUOLSLY DEPOSITED.
HYY -- 12/21/81
D-ANSCAT
VALIUE
(LAMBDA (NAME: CLINK: CO: NHORN: REG: MBNDG: FLG: MSG:)
(IF MSG:
(MAPC MGG: (LAMDUA (MSG) (SETO REG: (RECORD. DANS FEG: MSG))))
(SETA MSG: NIL)
(IF (AND FLG: (ALL-HORNS? REG: NHORN:))
(COND
((EO (REGFETCH CLTNK: "NAME:) *TOPMOST-TOFINF)
(D-SEND (DRAFT.D-ANS CQ: NHORN: REG:) CLINK:))
(T (SEND (DRAFT.D-ANS CQ: NHORN: REG:) CLINK:)))
(SETQ FLG: NIL)))
(SET CURNT: (LIST NAME: CLINK: CQ: NHORN: REG: MBNDG: FLG: MSG:)))
PLIST
(LREGS: (NAME: CLINK: CQ: NHORN: REG: MBNDG: FLG: MSG:))
****************************************************************
* [D-HORN?] ASKS IF OR NOT THE GIVEN NOLE CDNES IS A PPOTENTIALLY USEFUL
HORN FOR A DILEMMA INFERENCE. FOR THE TIME BEING, SDNE IS REGARDED
* AS A CANDIDATE HORN SET ONLY WHEN IT IS A DISJUNCTIUELY ASSERTED CONTAINING
* NO UARIABLES. FOR A FURTHER EXPANSION OF DILEMMA INFERENCE EVEN WITH RULE
* NODES, A RELAXATION OF THTS FUNCTION MUST BE APPROPRIATELY MADE.

I-HORN?

## VALUE

(LAMBDA (NDE)
(FROG (MINI)
(RETURN
(AND (TOPO NDE)
(NO-FREEUAR? NDE)
(NON-NILE (MAPCAR (GET NDE "ARG) ATOMOLECULE?)
(SETO MINI (CAR (GET NUE IMIN)))
(PLUSP (DIFF (LENGTH (GET NDE *ARG)) MINI)))))

PLIST
NIL

```
##*****************************************************************************
* [D-INFER] ITERATIVELY TRIES TO PROUE THE GIVEN CO WITH EACH HORN bEING
* AN ASSUMPTION.
HYY -- 12/21/81
```

        D-INFER
    VALUE
(LAMBDA (NAME: CLINK: CQ: HORNSET: MBNDG:)
(MAPC
(COR HORNEET:)
(LAMBDA (HORN)
(PROG (HP HC)
(SETQ
HP SNEN "ATTACK.HORN
(SETQ HC (NEW 'HORN-ANSCAT CLINK: (ARGN HORN 2) NIL NIL T))
(HORN-TORN-CQ HORN CQ:)
(UN1ON-B (ARGN HORN 2) MBNDG:)))
(REGSTORE CLINK: "REG: (CONS (LIST HC) (REGFETCH CLINK: 'REG:)))
(INITIATE HF)))),
PLIST
(LREGS: (NAME: CLTNK: CO: HORNSET: MBNDG:))
*************************************************************************

* [B-SEND] IS A KLUDGE FOR SENDING AN ANSHER DERTUED THROUGH A D-INFERENCE
* TO [TOPMOST-TOPINF] PROCESS. THE REASON FOR NOT USING NORMAL MESEAGE
* CHANNEL IS DESCRIBED IN LDEDUCE* I SECTION. THIS MUST BE, THOUCH, ELIMINATED
* IN THE FIITURE BY CHANGING SOME CODE IN [TOPMOST-TOPINF] PROCESS, THFOWING
* away the register si-ans:? eventually.
HYY -- 12/21/81
D-SEND
VALUE
(LAMBDA (ANS BOSS)
(SETQ ANS (CAR (ARGN ANS 2)))
(REGSTORE BOSS 'LI-ANS: ANS)
(INITIATE BOSS))
FLIST
NIL

* [DEOUCE*] MOOIFIEI BY HYY IN ORDER TO ADD ONE EXTRA REGISTOR TO THE PROCESS
* [TOPMOST-TOFINF]. THIS REGLSTOR IS NEEDED TO GET AN ANSWER FROM THE
* DILEmíA INFERENCING PROCESS. THE REASON WHY WE DO NOT USE THE NORTAL
* MESEAGE SENDTNG CHANNEL FOR THIS PURPOSE IS TO AVOTD THE THEOREM PROUEN
* via d-inference being permenantly built in the database.
HYY -- 12/21/81

```
        DEDUCE*
VALUE
(lambia (NumFLD CO)
    (PROG (TP RESULTS: INF %DILEMMA)
    (SETO %DILEMMA DILEMMA)
    (PUT 'LASTINFER":VAL NIL)
    (IF (NULL (FIRST-ATOM CO)) (RETURN RESULTS:))
    (SETO
        TP (NEN "TOPMOST-TOPINF
            NIL
            (FIRST-ATOM CO)
            NIL
            NIL
            0
            0
                (IF (NUMBERP NIMFLD) NUMFLD)
                (IF (NOT (ATOM NUMFLD)) (CAR NUMFLDD))
                    (IF (NOT (ATOM NUMFLD)) (CADR NUMFLD))
                NIL
                NIL
                    CNEW PI-MTR
                        NIL
                        (LIST (SETQ INF (NEW "INFER NIL (FIRST-ATOM CE) NIL NIL)))
                NIL)
            NIL))
        (REGSTORE INF 'CLINK: TP)
        (MULTIP (LIST (REGFETCH TP "MTR:)))
        (PUT 'LASTIGFER ':VAL (LIST TP))
        (TERPRI)
        (TERPRI)
        (RETURN RESULTE:)))
        PLIST
        NIL
    #**************************************************************************
    * [OILEM-RPT] ISSUES A SNEPSILL USER READABLE MESSAGE FOR THE DILEMMA INFERENCE
* FROCESSING TAKEN.
* HYY -- 12/21/81
        OILEM-RPT
value
(LAMBOA (HORNSET)
    (PRIN3 & "FOR A DILEMMA INFERENCE,")
    (COND ((EO (REGFETCH DOSS 'NAME:) "TOPMOST-TOPINF) (PRIN3 > " WE KNOW" >))
            (T (PRIN3 & " SINCE" >))
    (DESCRIBE (^ (CAR HORMSET))))
PLIST
NIL
#****************************************************************
* \OHTLEmm@> is a global SWItCH FOR dilEmma Inferencing. default is T.
* HYY -- 12/21/81
DILEMMA
value
T
PLIST
NIL
```

* LDLLEMMA-INFERJ I EFAHIVELY IKIES EVERY HORNSEI IAKEN FKOM IHE HORNPILE,
* SETIING UP [D-ANSCAT] FOR ANSER CATCHER AND [D-INFER] FOR A DISJUNCTIUE * REASONING.

```
        DILEMMA-INFER
valuE
(LAMBDA (BOSS CO MBNDG HORNPILE)
    (SETO %OILEMMA NIL)
    (FEPEAT NIL
        WHILE HORNPILE
            (DLLEM-RPT (CAR HORNPILE))
            (INITIATE {NEN 'D-INFER
                                    (NEW 3D-ANSCAT
                                    BOSS
                                    CQ:
                                    (LENGTH (CDAR HORNPILE))
                                    NIL
                                    MBNDG
                    T
                    NIL)
                    CQ
                        (CAR HORNPILE)
                            MIZNDG))
            (SETQ HORNPILE (COR HORNPTLE))))
PLIST
NIL
#**********************************************************************************
    * [DRAFT.D-ANS] IS A KLUDGE FOR SENDING AN ANSNER DUE TO DILEMMA INFERENCE
    * [DRAFT.D-ANS] DRAFTS THE FINAL ANSWER TO BE SENT TO LTOPMOST-TOPINF] WHEN
    * A DILEmmA INFERENCE BRINGS UP WITH A DISJUNCTIUE ANENER. NOTE THAT THE
    * ANENER IS A TEMPORARY NODE.
                                    HYY -- 12/21/81
        DRAFT:D-ANS
VALUE
(LAMBDA (CN MAXI REG)
    ILIST CO
        (APFLY TBUILD
                                    \LIST 'mAX
                                    MAXI
                                    MMIN
                            \perp
                            * ARG
                            (MAPCAR REG (LAMBDA (D-ANS) (NBUILD CQ (CALR D-ANS) TBUILD)))))))
```


## FLIST

NIL

EQUISET

## VALUE

(LAMBDA (i.1 L2)
(AND (EO (LENGTH L1) (LENGTH L2))
(NON-NILS (MAFCAR Li (LAMBGA (LL) (MEMB LL L2))))))

## PLIST

NIL

LGHIHER.HOKNS GHIHENE WOKIHWHLE HORN-SETS FOR H DLLEMMA INFERENCE OF THE
GIVEN CO. A HORN-SET IS A DISJUNCTIUELY ASSERTED STATEMENT IN WHICH ANY

* SUBSET OF THE GIVEN CA IS INCLIEDED AS ONE OF ITS DISJUNTS.
* RETURZS (MI (MJ BJ TJ) (MK BK TK) ....),
* Where mi Is the mode of the horneet found in the database, (MJ."TJ) IS A DATA SET FOR EACH HORN, WHERE, MU IS THE NODE OF HOFN DISUUNCT,

BU IS THE GINGING SATISFYING THE HORN AS AN ASSIMPTION, TU IS THE SUG-PART OF CO WHICH IS PROUED BY THE HORN ASSUMPTION. HYY -- 12/21/81

GATHER.HORNE
VALUE
(LAMEDA (CN BNDG)
(PROG (HRN)
(MAPC (OR (GET CO 'ARG) \{LIST CO))
(LAMBDA (X)
(MAPC (MATCHI $X$ BNDG)
(LAMBDA (Y) (SETO HRN (CONS (APPEND Y (LIST X)) HRN)))))
(RETURN (SORT.HORNS (PUTIT-BASEET (SELECT.HORNS HRN)))) ))

## PLIST

NIL


* [HORN-ANSCAT] CATCHES ANSWERS FOR A HORN AND SEND THE FIRET ANENER TO * [D-ANGCATI. RIOHT NOW, THE ANSWER IS SENT JUST ONCE. IN THE FITURE, * SOMEONE MAY ATTEMPT TO LET IT SEND ALL ANSWERS BACK. BUT NOTLCE THAT * A TAXONOMICALLY EMDEDDED DTSUUNCTION OF DISUNCTIONS ARE REALLY MESSY.

HORP-ANSCAT
VALIIE
(LAMBDA (NAME: CLINK: BNDG: FEG: HSG: FLG:)
(IF HSG: (SETQ REG: (AFPEND REG: (CDR MSG:)) MSG: NIL))
(IF FLG* (SEND (LIST CURNT: (UNION-B BNDG: (CAR REG:))) CLINK:) (SETO FLG: NIL)) (SET CURNT: (LIST NAME: CLINK: BNDG: REG: MSG: FLG:)))

PLIST
(LREGS: (NAME: CLTNK: BNDG: REG: MSG: FLG:))

## 

* [HORN-TORN-CA] GENERATES A NEW CN TO BE PROVED FROM A GIUEN CO WITH THE
* ASSIMPTION THAT THE HORN IS TRUE.
* returns a temporary node nehly butlt.
HYY -- 12/21/81

HORN-TORN-CO
VALUE
(LAMBDA (HOFN CO)
(PROG (LCO)
(RETURN
COOND
( (OR (EO CQ (ARGN HORN 3)) (EN (SETO LCO (LENGTH (GET CO PARG))) 1)) NIL) (T \{FIRST-ATOM (APPLY TBUILD
(LIST 'MAX
( $\operatorname{BUBL} \mathrm{LCO}$ )
9MIN
(SUBL LCO)
: ARG
(INTORN-CO (ARGN HORN 3) (GET CO *ARG)))))) ))

## * [INFER] MODIFIED BY HYY $12 / 21 / 91$

* in order to collect hofnsets into a hornpile, and call dilemma inferenctng
* FOUTINE IF CDLLEMMAS IS SET AND CHORNPTLE IS NOT EMPTY. FOR THE TIME bETNG
* CDILEMMA. IS SET TO NIL AT ALL EMDEDDED INFERENCE LEUELS. HOMEUER, THIS MAY
* BE LIFTED IN THE FUTURE IF AN ENOUGH HOTTVATION JUSTIFTES TO DO SO.
* SNITCHING OF CDILEMAS IS DONE IN [ULLEMAA-INFER].

INFER
VALIE
(LAMBDA (NAME: CLINK: CQ: BNUG: MSGZ)
(PROG (WD HORNPTLE)
(COND
(ANL (NULL MSG:) (GET CQ: "NAME:))
(INITIATE (NEW 'EVAL-FN CLINK: CQ: BNDG: NIL NIL))) (T)
(PROG (M A D)
(SETQ M (OR MSG: (MATCHI CO: BNDG:)) MSG: NIL)
(EETQ WO (WORTH-DIL? CQ:))
(IF (AND \%DILEMMA WH) (SETO HORNPILE (GATHER.HORNS CR: BNDG:))
(FEPEAT NIL
WHILE M
(COND
((TOP? (TNODE (CAR M)))
(SETA A (CONS (LTET (TNODE (CAR M)) (SBIND (CAR M))) A))
(IF (EO (REGFETCH CLINK: 'NAME:) "TOPMOST-TOPINF)
(INF-RPT (SBIND (CAR M)) NIL NIL (LIST CQ:D)))
( (AND (OR (GET (TNODE (CAR H)) (CONU "CQ))
(GET (TNODE (CAR M)) (CONU "ARC))
(GET (TNODE (CAR M)) (CONU 'DCO)))
(NOT
(MEMBER
NIL
(MAPCAR (TBIND (CAR M))
(LAMBDA (BP)
(OR (VAR (CDR BP))
(AIULL (GET (CAR BP) 'EUB-))) )) ))
(SETA $0(C O N S$ (CAR M) D)) ))
(CETOM (COR M)))
(IF OR A
(AND (NULL (REGFETCH CLINK: 'CLINK:))
(ERP (REGFETCH CLINK: 'TOT:) O))
(SEND (CONS CO: A) CLINK: ) )
(IF (AND D (OR (NULL A) (WH-O (SUAR CO:) BNDG:)))
MAPC D
(LAMBDA (MTCHD)
(INITIATE
(NEN 'GO-HP
(NEH SWITCH CLINK: CO: (EBIND MTCHD) NIL) (TNODE MTCHD)
(TBIND MTCHD)))) ) )
(IF (AND \%DLLEMMA WD HORNPILE) (DILEMMA-INFER OLIN:: CO: BNDG: HORNPTLE)) (COND
(CGET CA: MAX)
(INITIATE

```
            (DEI LS: "ANG)
                BNDG:
                    NIL
                    NIL)))
            ((GET CO: 'I-//-) (INTYIGTE (NEH *UI-//- CLINK: CO: BNDG: NIL NIL)))
            ({GET CO: ,UNK\ (INITIATE (NEW "U-UNK: CLINK: CO: BNLG: NIL NTL NIL NTL))))))
            (SET CURNT: (LTST NAME: CLTNK: CO: BNDG: MSG:))))
PLIST
(LREGS: (NAME: CLINK: CQ: BNDG: MSG:))
    NO-FREEUAR:
VALUE
(LAMBDA (NDE)
    (NON-NILS (MAPCAR (DOWNSET NLE) (LAMBDA (X) (NOT (UAR (CDR X))))))
PLIST
NIL
```

```
############********************************************************************
* [NON-NILS] IS A HELP FINCTION TESTING IF A LIST CONTATNS ANY TOP LEUEL NIL
* AS AN ELEMENT. THIS IS USEFLL USED ASSOCIATED WITH A [MAPCAR] FUNCTION.
                                    HYY -- 12/21/81
        NON-NTLS
VALUE
(LAMBDA (LST)
    (COND (\NILL LST) T)
            ((NULL (CAR LST)) NIL)
            (T (AND (CAR LST) (NON-NILS (COR LST))))))
```


## PLIST

```
N1L
```


## 

```
* [PACK-IN] IS AN AID TO [PUTIN-BASKET]
```

                                    HYY -- 12/21 (PROG (TND)
    ```
                                    HYY -- 12/21 (PROG (TND)
(RETURN
(COND
( (NULL HHEAP) NTL)
( (AND (MEMB (SETO TND (CAR (GET (CAAR HHEAP) (CONV 'ARG))))
(GET NODES : VARL)
(D-HOFN? TND)
(CONS (LIST TND (CAAR HHEAP) (ARGN (CAR HHEAF) 3) (ARGN (CAR HHEAP) A)) (SELECT.HORNS (CDR HHEAP))))
( \((\) (SELECT. HORNS (CDR HHEAP))))) ))
```


## PLIST

NIL

## SET. PREG

VALIE
(LAMBDA (FL)
(HAPC FL (LAMBDA (F) (PUT F ILREGS: (ARGN (EVAL F) 2)))) (APPLY OUTPUT (LIST 'DILMA FL)))

## PLIST

NIL

## 

* [SORT.HORNS] PUTS ALL USEFIL HORNS SELECTED BY [SELECT.HORNS] INTO A

SORT. HORNE
VALUE
(LAMBLA (HORNE)
(PROG (HORNPILE)
(MAPC HORNS
(LAMBDA (HSET)
(IF (EQUISET (GET (CAR HSET) 'ARG) (MAPCAR (CLR HSET) CAR)) (SETO HORNPILE (CONS HSET HORNPILE)))))
(RETURN HORNPTLE))

```
PLIST
```

NLL

## 

## * [TOPMOST-TOPINF] MODIFIED BY HYY ON $12 / 21 / 81$

* IN ORUER TO ADD AN EXTFA REGISTOR CD-ANS: THAT WTLL RECETVE AN ANSHER
* FROH A OLLEMMA INFERENCE ROUTINE. SHOULD BE FURTHER IMPROUED IN THE FUTIIRE.

```
    TOPMOST-TOPINF
VALUE
\LAMBDA <NAME: CLINK: CQ: DATA: MSG: N-ANS: P-ANS: TOT: N-POS
    (1F D-ANS:
    (PRIN3 > " HERE, HE INFER A DISUUNCTIUE ANSWER" ) 
    (APPLY DESCRIBE D-ANS:)
    (SETQ L-ANS: NIL))
    (IF (SETO HSG: (MEMBER-S (MAPCONC MSG: (LAMBDA (X) (COR X))) (SBINDS DATA:)))
    (SEND MSG: BOSSES:)
    (SETO DATA: (APPEND DATA: MSG:))
    MMAPC
        (MAPCAR MSG:
            (LAMBDA (X)
                            (CONS (FIRST-ATOM (NBUILD (COND ((SAME-SIGN (CAR X) CO:) CN:)
                                    (T (NEGATE CQ:)))
                                    (CADR X)
                                    FORBTOP))
                                    (COR X))))
        \LAMBDA (ANS)
            (IF (NOT (MEMBER (CAR ANS) RESULTS:))
            (SETO RESILTS: (SNOC RESILTS: (CAR ANS))))
        (COND ((NEGATED (CAR ANS)) (SETO N-ANS: (ADDI N-ANS:)))
            (T (SETO P-ANS: (ADD1 P-ANS:))))))
    (IF (NOT (CONT? N-ANS: P-ANS: TOT: N-POS: N-NEG:))
        \SETO
        /HSUSPSH (APPEND
            /$SUSPS*
            MMAPCONC
                (APPEND SUSPS: EVNTS)
                (LAMBDA (E)
                    (IF (OR (BELOWP E CURNT:)
                                    (MEMBER (FEGFETCH E 'NAME:) "(I-MTR I-MTR-R)))
                            (LTSTED))))
        EUNTS (MAPCONC EUNTS (LAMBUA (E) (IF (NOT (MEMBER E/HSUSPSH)) (LIST E))))
        SUSPS: (MAPCONC SUSPS: (LAMBDA (E) (IF (NOT (MEMBER E /HSUSPSN)) (LIST E))))
        (IF (EO TP CLIRNT:)
            (MAPC EUNTS (LAMBDA (X) (SUSPEMDEM X)))
            (MAPC SUSPS: (LAMBOA ( }X\mathrm{ ( (SUSPENDEM X)))
            (SETQ EUNTS NIL SUSPS: NIL)))
    (SETO MSG: NTL))
    SEET CURNT:
```


## $L+$



DHIA: MSG:

## NS:

## PLIST



## 

* [UNTORN-CO] HELPS [HORN-TORN-CQ] TO GENERATE A NEW CO TO BE PROUEO. * [UNTORN-CO] RETUFNS A LIST OF NODES DISTINCT FROM HORN NODE.
* HYY -- 12/21/81

```
        UNTORN-CO
VALUE
(LAMBDA (HCO CO)
    (COND ((EQ (CAR CO) HCQ) (CDF CO))
            (T (CONS (CAR CN) (UNTORN-CO HCO (COR CO)))))
```

PLIST
NIL


* [WORTH-DIL?] TESTS IF OR NOT A DILEMMA INFERENCING IS WORTH TO BE EVER
* ATTEMPTED FOR THE GIUEN ©CO. NO D-INFERENCE IE ATTEMPTED FOR AN ALREADY
* DISUUNCTIUE QUERY:
* HYY - $-12 / 21 / 81$
WORTH-OIL?
VALUE
(LAMBDA (CN)
(PROG (MAXI)
GRETURN
(OR (AND (SETO MAXI (CAR (GET CO "MAX)))
(EQ MAXI (CAR (GET CQ MMIN)))
(NON-NILS (MAPCAR (GET CO 'ARG) ATOMOLECILE?))
(ATOMOLECULE? CQ))) )


## PLIST

NIL

## CROSS REFERENCE OF DILMA

| ALL-HORNS? | D-ANSCAT |
| :--- | :--- |
| ATOMOLECULE? | D-HOFN? WORTH-DML? |
| ATTACK.HORN | D-INFER |
| D-GNGCAY | DILEMMA-INFER |
| D-HORN? | SELECT.HORNS |
| D-INFER | DTLEMMA-INFER |
| D-SEND | D-ANSCAT |
| DEDUCE* | DILEMMA-INFER |

```
DILEMMA-TNFER INFER
DRAFT.D-ANS D-ANSCAT
EOUISET SORT.HORNS
GATHER.HORNS INFER
HORN-ANSCAT D-INFER
HORN-TORN-CO D-INFER
INFER DEDUCE*
NO-FREEVAR? D-HORN?
NON-NILS ALL-HORNS? ATOMOLECULE? D-HORN? EQUTSET
    NO-FREEUAR? NON-NILS WORTH-DLL?
FACK-IN PACK-IN PUTIN-BASKET
PITIN-BASKET GATHEF.HORNS
RECORD.DANS I-ANSCAT RECORD.DANS
SELECT.HORNS GATHER.HOFNS SELECT.HORNS
SET.PREG
SORT.HORNS GATHER.HORNE
TOPMOST-TOPINF D-ANSCAT DEDUCE* DILEM-RPT INFER
UNTORN-CN HORN-TORN-CN INTORN-CQ
HOFTH-DIL? INFER
NIL
    ?(EXIT)
REUERT.
/
```

