Relational Databases

Jan Chomicki
University at Buffalo

Relational data model

Relational data model

Domain

- domain: predefined set of atomic values: integers, strings,...
- every attribute value comes from a domain or is null (null is not a value)
- First Normal Form: domains consist of atomic values

Relational data model

Domain

- domain: predefined set of atomic values: integers, strings,...
- every attribute value comes from a domain or is null (null is not a value)
- First Normal Form: domains consist of atomic values

Tuple (row)

- tuple: a sequence of values and nulls
- tuple arity: the number of values in the sequence (including nulls)

Relational data model

Domain

- domain: predefined set of atomic values: integers, strings,...
- every attribute value comes from a domain or is null (null is not a value)
- First Normal Form: domains consist of atomic values

Tuple (row)

- tuple: a sequence of values and nulls
- tuple arity: the number of values in the sequence (including nulls)

Relation

- relation name, e.g., `Employee`
- relation schema: finite set of attributes (column labels) and associated domains, for example

  `Name:String`, `Salary:Decimal`, `Age:Integer`

- relation instance: finite set of tuples conforming to the schema.

Schema vs. instance

Schema vs. instance

Schema

- rarely changes
- when it does, database needs to be reorganized
- used to formulate queries

Schema vs. instance

Schema

- rarely changes
- when it does, database needs to be reorganized
- used to formulate queries

Instance

- changes with update transactions
- used to evaluate queries

Notation

An instance of a schema R is denoted r.

Schema vs. instance

Schema

- rarely changes
- when it does, database needs to be reorganized
- used to formulate queries

Instance

- changes with update transactions
- used to evaluate queries

Notation

An instance of a schema R is denoted r.

We will need the schema vs. instance distinction in discussing integrity constraints and query results.

Integrity constraints

Logical conditions that have to be satisfied in every database instance.

Integrity constraints

Logical conditions that have to be satisfied in every database instance.

Role of constraints

- guarding against entering incorrect data into a database (data quality)
- providing object identity (key and foreign key constraints)
- representing relationships and associations
- helping in database design

Integrity constraints

Logical conditions that have to be satisfied in every database instance.

Role of constraints

- guarding against entering incorrect data into a database (data quality)
- providing object identity (key and foreign key constraints)
- representing relationships and associations
- helping in database design

DBMS support for constraints

- all declared constraints are checked after every transaction
- if any constraint is violated, the transaction is backed out
- typically SQL DBMS support only limited kinds of constraints
  - keys, foreign keys, CHECK constraints

Key constraints

Key constraints

Key constraint of a relation schema R

A set of attributes S (called a key) of R.

Key constraints

Key constraint of a relation schema R

A set of attributes S (called a key) of R.

An instance r satisfies a key constraint S if r does not contain a pair of tuples that agree on S but disagree on some other attribute of R.

Key constraints

Key constraint of a relation schema R

A set of attributes S (called a key) of R.

An instance r satisfies a key constraint S if r does not contain a pair of tuples that agree on S but disagree on some other attribute of R.

Formally: for each two tuples $t_1 \in r$, $t_2 \in r$

$$\textit{if } t_1[S] = t_2[S], \textit{ then } t_1[A] = t_2[A] \textit{ for every attribute } A \textit{ in } R.$$

Properties of keys

Properties of keys

Adequacy

- uniqueness of key values should be guaranteed by the properties of the application domain
- in other words: it is an error to have different tuples (in the same relation) with the same key values
- a key should be as small as possible (good database design)

Properties of keys

Adequacy

- uniqueness of key values should be guaranteed by the properties of the application domain
- in other words: it is an error to have different tuples (in the same relation) with the same key values
- a key should be as small as possible (good database design)

Minimality

- no subset of a key can also be designated a key

Properties of keys

Adequacy

- uniqueness of key values should be guaranteed by the properties of the application domain
- in other words: it is an error to have different tuples (in the same relation) with the same key values
- a key should be as small as possible (good database design)

Minimality

- no subset of a key can also be designated a key

Multiple keys

- there may be more than one key in a relation schema
- one is selected as the primary key:
  - cannot be null (entity integrity)
  - typically used in indexing

Relational model is value-based

Relational model is value-based

No duplicates

There cannot be two different "objects" (here: tuples) whose all attribute values are pairwise equal.

Relational model is value-based

No duplicates

There cannot be two different "objects" (here: tuples) whose all attribute values are pairwise equal.

No pointers

The only way to reference an "object" (tuple) is by providing its key value.

Relational model is value-based

No duplicates

There cannot be two different "objects" (here: tuples) whose all attribute values are pairwise equal.

No pointers

The only way to reference an "object" (tuple) is by providing its key value.

No notion of *location*

It is not possible to refer to the location of an object (tuple).

Relational model is value-based

No duplicates

There cannot be two different "objects" (here: tuples) whose all attribute values are pairwise equal.

No pointers

The only way to reference an "object" (tuple) is by providing its key value.

No notion of *location*

It is not possible to refer to the location of an object (tuple).

These properties are *not* shared by the ER model, object-oriented models, XML etc.

Foreign keys

Relation schemas R_1, R_2 (not necessarily distinct).

Foreign keys

Relation schemas R_1, R_2 (not necessarily distinct).

Foreign key constraint

A pair of sets of attributes (S_1, S_2) such that:

- $S_1 \subseteq R_1$, $S_2 \subseteq R_2$
- S_2 is a key of R_2
- the number of attributes and their respective domains in S_1 and S_2 are the same.

Foreign keys

Relation schemas R_1, R_2 (not necessarily distinct).

Foreign key constraint

A pair of sets of attributes (S_1, S_2) such that:

- $S_1 \subseteq R_1$, $S_2 \subseteq R_2$
- S_2 is a key of R_2
- the number of attributes and their respective domains in S_1 and S_2 are the same.

A pair of instances (r_1, r_2) satisfies a foreign key constraint (S_1, S_2)

if for every tuple $t_1 \in r_1$, $t_1[S_1] = t_2[S_2]$ for some tuple $t_2 \in r_2$ or $t_1[S_1]$ is null.

Foreign keys

Relation schemas R_1, R_2 (not necessarily distinct).

Foreign key constraint

A pair of sets of attributes (S_1, S_2) such that:

- $S_1 \subseteq R_1$, $S_2 \subseteq R_2$
- S_2 is a key of R_2
- the number of attributes and their respective domains in S_1 and S_2 are the same.

A pair of instances (r_1, r_2) satisfies a foreign key constraint (S_1, S_2)

if for every tuple $t_1 \in r_1$, $t_1[S_1] = t_2[S_2]$ for some tuple $t_2 \in r_2$ or $t_1[S_1]$ is null.

A primary key (or a part thereof) can be a foreign key at the same time (but then it can't be null).

Other kinds of integrity constraints?

Other kinds of integrity constraints?

Functional dependencies

- generalize key constraints

Other kinds of integrity constraints?

Functional dependencies

- generalize key constraints

Inclusion dependencies

- generalize foreign key constraints

Other kinds of integrity constraints?

Functional dependencies

- generalize key constraints

Inclusion dependencies

- generalize foreign key constraints

Multivalued dependencies

Other kinds of integrity constraints?

Functional dependencies

- generalize key constraints

Inclusion dependencies

- generalize foreign key constraints

Multivalued dependencies

All rarely supported by current DBMS.

Logical conditions

Logical conditions

General conditions

- essentially queries
- shouldn't evaluate to False in any valid instance

Logical conditions

General conditions

- essentially queries
- shouldn't evaluate to False in any valid instance

> *"I'm willing to admit that I may not always be right, but I am never wrong."*
>
> *Samuel Goldwyn*

Logical conditions

General conditions

- essentially queries
- shouldn't evaluate to False in any valid instance

> *"I'm willing to admit that I may not always be right, but I am never wrong."*
>
> *Samuel Goldwyn*

Scope

- can be associated with attributes, tuples, relations, or databases
- SQL DBMS often implements only tuple-level conditions (`CHECK` constraints)

Relational query languages

Relational query languages

Relational algebra

- a set of algebraic operator
- each operator takes one or two relations as arguments and returns a relation as the result
- operators can be nested to form expressions
- procedural query language: expressions describe how the query can be evaluated

Relational query languages

Relational algebra

- a set of algebraic operator
- each operator takes one or two relations as arguments and returns a relation as the result
- operators can be nested to form expressions
- procedural query language: expressions describe how the query can be evaluated

Relational calculus

- a logic language: expressions involve Boolean operators and quantifiers
- declarative query language: expressions do not describe how to evaluate the query
- we will not talk about it

Relational query languages

Relational algebra

- a set of algebraic operator
- each operator takes one or two relations as arguments and returns a relation as the result
- operators can be nested to form expressions
- procedural query language: expressions describe how the query can be evaluated

Relational calculus

- a logic language: expressions involve Boolean operators and quantifiers
- declarative query language: expressions do not describe how to evaluate the query
- we will not talk about it

SQL

- a mix of relational algebra and logic (procedural/declarative)
- the standard query language of the existing DBMS.

Subtle issues

Subtle issues

Nulls

- relational algebra does not allow nulls
- SQL does

Subtle issues

Nulls

- relational algebra does not allow nulls
- SQL does

Duplicates

- relational algebra operates on sets and does not allow duplicates
- SQL allows duplicates and operates on multisets (bags)
- duplicates irrelevant for most queries

Subtle issues

Nulls

- relational algebra does not allow nulls
- SQL does

Duplicates

- relational algebra operates on sets and does not allow duplicates
- SQL allows duplicates and operates on multisets (bags)
- duplicates irrelevant for most queries

Order

- neither relational algebra nor SQL can specify order within sets of tuples
- in SQL top-level query results can be ordered
  - but not in subqueries

Basic operators

Basic operators

Set operators

- union
- set difference

Basic operators

Set operators

- union
- set difference

Relational operators

- Cartesian product
- selection
- projection
- renaming.

Basic operators

Set operators

- union
- set difference

Relational operators

- Cartesian product
- selection
- projection
- renaming.

This is a minimal set of operators.

Union and difference

Union and difference

Union ($\cup$) of R_1 and R_2

- $arity(R_1 \cup R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 \cup r_2$ iff $t \in r_1$ or $t \in r_2$.

Union and difference

Union ($\cup$) of R_1 and R_2

- $arity(R_1 \cup R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 \cup r_2$ iff $t \in r_1$ or $t \in r_2$.

Difference ($-$) of R_1 and R_2

- $arity(R_1 - R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 - r_2$ iff $t \in r_1$ and $t \notin r_2$.

Union and difference

Union ($\cup$) of R_1 and R_2

- $arity(R_1 \cup R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 \cup r_2$ iff $t \in r_1$ or $t \in r_2$.

Difference ($-$) of R_1 and R_2

- $arity(R_1 - R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 - r_2$ iff $t \in r_1$ and $t \notin r_2$.

The arguments of union and difference need to be compatible.

Union and difference

Union ($\cup$) of R_1 and R_2

- $arity(R_1 \cup R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 \cup r_2$ iff $t \in r_1$ or $t \in r_2$.

Difference ($-$) of R_1 and R_2

- $arity(R_1 - R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 - r_2$ iff $t \in r_1$ and $t \notin r_2$.

The arguments of union and difference need to be compatible.

Compatibility of R_1 and R_2

- $arity(R_1) = arity(R_2)$
- the corresponding attribute domains in R_1 and R_2 are the same
- thus compatibility of two relations can be determined solely on the basis of their schemas (compile-time property).

Cartesian product of R_1 and R_2

$arity(R_1) = k_1$, $arity(R_2) = k_2$

Cartesian product($\times$)

- $arity(R_1 \times R_2) = arity(R_1) + arity(R_2)$
- $t \in r_1 \times r_2$ iff:
  - the first k_1 components of t form a tuple in r_1, and
  - the next k_2 components of t form a tuple in r_2.

Selection

Selection condition E built from:

- comparisons between operands which can be constants or attribute names
- Boolean operators: $\wedge$ (AND), $\vee$ (OR), $\neg$ (NOT).

Selection $\sigma_E(R)$

- $arity(\sigma_E(R)) = arity(R)$
- $t \in \sigma_E(r)$ iff $t \in r$ and t satisfies E.

Projection

$A_1, \ldots, A_k$: distinct attributes of R.

Projection $\pi_{A_1,\ldots,A_k}(R)$

- $arity(\pi_{A_1,\ldots,A_k}(R)) = k$
- $t \in \pi_{A_1,\ldots,A_k}(r)$ iff for some $s \in r$, $t[A_1 \ldots A_k] = s[A_1 \ldots A_k]$.

Renaming

$A_1, \ldots, A_n$: attributes of R
$B_1, \ldots, B_n$: new attributes

Renaming $R(B_1, \ldots, B_n)$

- $arity(R(B_1, \ldots, B_n)) = arity(R) = n$,
- $t \in r(B_1, \ldots, B_n)$iff for some $s \in r$, $t[B_1 \ldots B_n] = s[A_1 \ldots A_n]$.

Derived operators

1. Intersection.
2. Quotient.
3. θ-join.
4. Natural join.

Intersection

Intersection

- $arity(R_1 \cap R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 \cap r_2$ iff $t \in r_1$ and $t \in r_2$.

Intersection

Intersection

- $arity(R_1 \cap R_2) = arity(R_1) = arity(R_2)$
- $t \in r_1 \cap r_2$ iff $t \in r_1$ and $t \in r_2$.

Intersection is a derived operator:

$$R_1 \cap R_2 = R_1 - (R_1 - R_2).$$

Quotient

$A_1, \ldots, A_{n+k}$: all the attributes of R_1
$A_{n+1}, \ldots, A_{n+k}$: all the attributes of R_2
r_2 nonempty.

Quotient (division)

- $arity(R_1 \div R_2) = arity(R_1) - arity(R_2) = n$
- $t \in r_1 \div r_2$ iff for all $s \in r_2$ there is a $w \in r_1$ such that
  - $w[A_1 \ldots A_n] = t[A_1 \ldots A_n]$, and
  - $w[A_{n+1} \ldots A_{n+k}] = s[A_{n+1} \ldots A_{n+k}]$.

Quotient

$A_1, \ldots, A_{n+k}$: all the attributes of R_1
$A_{n+1}, \ldots, A_{n+k}$: all the attributes of R_2
r_2 nonempty.

Quotient (division)

- $arity(R_1 \div R_2) = arity(R_1) - arity(R_2) = n$
- $t \in r_1 \div r_2$ iff for all $s \in r_2$ there is a $w \in r_1$ such that
  - $w[A_1 \ldots A_n] = t[A_1 \ldots A_n]$, and
  - $w[A_{n+1} \ldots A_{n+k}] = s[A_{n+1} \ldots A_{n+k}]$.

Quotient is a derived operator:

$$R_1 \div R_2 = \pi_{A_1,\ldots,A_n}(R_1) - \pi_{A_1,\ldots,A_n}(\pi_{A_1,\ldots,A_n}(R_1) \times R_2 - R_1)$$

θ-join

θ: a comparison operator $(=, \neq, <, >, \geq, \leq)$
$A_1, \ldots, A_n$: all the attributes of R_1
$B_1, \ldots, B_k$: all the attributes of R_2

θ-join

- $arity(R_1 \underset{A_i \theta B_j}{\bowtie} R_2) = arity(R_1) + arity(R_2)$
- $R_1 \underset{A_i \theta B_j}{\bowtie} R_2 = \sigma_{A_i \theta B_j}(R_1 \times R_2)$

θ-join

θ: a comparison operator $(=, \neq, <, >, \geq, \leq)$
$A_1, \ldots, A_n$: all the attributes of R_1
$B_1, \ldots, B_k$: all the attributes of R_2

θ-join

- $arity(R_1 \underset{A_i \theta B_j}{\bowtie} R_2) = arity(R_1) + arity(R_2)$
- $R_1 \underset{A_i \theta B_j}{\bowtie} R_2 = \sigma_{A_i \theta B_j}(R_1 \times R_2)$

Equijoin

θ-join where θ is equality.

Natural join

$A_1, \ldots, A_n$: all the attributes of R_1
$B_1, \ldots, B_k$: all the attributes of R_2
m - the number of attributes common to R_1 and R_2

Natural join

- $arity(R_1 \bowtie R_2) = arity(R_1) + arity(R_2) - m$
- to obtain $r_1 \bowtie r_2$:
  1. select from $r_1 \times r_2$ the tuples that agree on all attributes common to R_1 and R_2
  2. project duplicate columns out from the resulting tuples.

Query evaluation

Query evaluation

Basic

- queries evaluated bottom-up: an operator is applied after the arguments have been computed
- temporary relations for intermediate results

Query evaluation

Basic

- queries evaluated bottom-up: an operator is applied after the arguments have been computed
- temporary relations for intermediate results

Advanced

- using indexes, sorting and hashing
- special algorithms
- input/output streams, blocking
- parallelism

SQL

Support

- virtually all relational DBMS
- vendor-specific extensions

Standardized (partially)

- SQL2 or SQL-92 (completed 1992)
- SQL3, SQL:1999, SQL:2003 (completed)
- SQL:2006 (ongoing work)

SQL language components

- query language
- data definition language
- data manipulation language
- integrity constraints and views
- API's (ODBC, JDBC)
- host language preprocessors (Embedded SQL, SQLJ)
- support XML data and queries
- ...

Basic SQL queries

Basic form

SELECT $A_1, \ldots, A_n$
FROM $R_1, \ldots, R_k$
WHERE C

Corresponding relational algebra expression

$$\pi_{A_1,\ldots,A_n}(\sigma_C(R_1 \times \cdots \times R_k))$$

Range variables

To refer to a relation more than once in the `FROM` clause, range variables are used.

Example

```
SELECT R1.A, R2.B
FROM R R1,R R2
WHERE R1.B=R2.A
```

corresponds to

$$\pi_{A,D}(R(A,B) \underset{B=C}{\bowtie} R(C,D)).$$

Manipulating the result

`SELECT *`: all the columns are selected.

`SELECT DISTINCT`: duplicates are eliminated from the result.

`ORDER BY` $A_1, \ldots, A_m$: the result is sorted according to $A_1, \ldots, A_m$.

E `AS` A can be used instead of an column A in the `SELECT` list to mean that the value of the column A in the result is determined using the (arithmetic or string) expression E.

Set operations

`UNION`	set union.
`INTERSECT`	set intersection.
`EXCEPT`	set difference.

Note

- `INTERSECT` and `EXCEPT` can be expressed using other SQL constructs

Nested queries

Nested queries

Subquery

A query Q can appear as a subquery in the `WHERE` clause which can now contain:

- A `IN` Q: for set membership ($A \in Q$)
- A `NOT IN` Q: for the negation of set membership ($A \notin Q$)
- $A\ \theta$ `ALL` Q: A is in the relationship θ to all the elements of Q ($\theta \in \{=, <, >, >=, <=, <>\}$)
- $A\ \theta$ `ANY` Q: A is in the relationship θ to some elements of Q
- `EXISTS` Q: Q is nonempty
- `NOT EXISTS` Q: Q is empty

Nested queries

Subquery

A query Q can appear as a subquery in the `WHERE` clause which can now contain:

- A `IN` Q: for set membership ($A \in Q$)
- A `NOT IN` Q: for the negation of set membership ($A \notin Q$)
- $A\ \theta$ `ALL` Q: A is in the relationship θ to all the elements of Q ($\theta \in \{=, <, >, >=, <=, <>\}$)
- $A\ \theta$ `ANY` Q: A is in the relationship θ to some elements of Q
- `EXISTS` Q: Q is nonempty
- `NOT EXISTS` Q: Q is empty

Notes

- the subqueries can contain columns from enclosing queries
- multiple occurrences of the same column name are disambiguated by choosing the closest enclosing `FROM` clause.

Aggregation

Aggregation

Instead of a column A, the `SELECT` list can contain the results of some aggregate function applied to all the values in the column A in the relation.

Aggregation

Instead of a column A, the `SELECT` list can contain the results of some aggregate function applied to all the values in the column A in the relation.

Aggregation functions

- `COUNT(`A`)`: the number of all values in the column A (with duplicates)
- `SUM(`A`)`: the sum of all values in the column A (with duplicates)
- `AVG(`A`)`: the average of all values in the column A (with duplicates)
- `MAX(`A`)`: the maximum value in the column A
- `MIN(`A`)`: the minimum value in the column A.

Aggregation

Instead of a column A, the `SELECT` list can contain the results of some aggregate function applied to all the values in the column A in the relation.

Aggregation functions

- `COUNT(`A`)`: the number of all values in the column A (with duplicates)
- `SUM(`A`)`: the sum of all values in the column A (with duplicates)
- `AVG(`A`)`: the average of all values in the column A (with duplicates)
- `MAX(`A`)`: the maximum value in the column A
- `MIN(`A`)`: the minimum value in the column A.

Notes

- `DISTINCT` A, instead of A, considers only distinct values
- aggregation queries not expressible in relational algebra

Grouping

Grouping

The clause

`GROUP BY` $A_1, \ldots, A_n$

assembles the tuples in the result of the query into groups with identical values in columns $A_1, \ldots, A_n$.

Grouping

The clause

`GROUP BY` $A_1, \ldots, A_n$

assembles the tuples in the result of the query into groups with identical values in columns $A_1, \ldots, A_n$.

The clause

`HAVING` C

leaves only those groups that satisfy the condition C.

Grouping

The clause

`GROUP BY` $A_1, \ldots, A_n$

assembles the tuples in the result of the query into groups with identical values in columns $A_1, \ldots, A_n$.

The clause

`HAVING` C

leaves only those groups that satisfy the condition C.

Notes

The `SELECT` list of a query with `GROUP BY` can contain only:

- the columns mentioned in `GROUP BY` (or expressions with those), or
- the result of an aggregate function, which is then viewed as applied group-by-group.

Building complex queries

Building complex queries

A complex query can be broken up into smaller pieces using:

- nested queries in the `FROM` clause
- views.

Building complex queries

A complex query can be broken up into smaller pieces using:

- nested queries in the `FROM` clause
- views.

View

Computed relation whose contents are defined by an SQL query.

Building complex queries

A complex query can be broken up into smaller pieces using:

- nested queries in the `FROM` clause
- views.

View

Computed relation whose contents are defined by an SQL query.

Creating a view

`CREATE VIEW` *View-name*(*Attr1*,...,*Attrn*)
`AS` *Query*

Building complex queries

A complex query can be broken up into smaller pieces using:

- nested queries in the `FROM` clause
- views.

View

Computed relation whose contents are defined by an SQL query.

Creating a view

`CREATE VIEW` *View-name*(*Attr1*,...,*Attrn*)
`AS` *Query*

Dropping a view

`DROP VIEW` *View-name*

Nulls

Nulls

Various interpretations: unknown, missing value, inapplicable, no information...

Nulls

Various interpretations: unknown, missing value, inapplicable, no information...

In SQL columns that are not explicitly or implicitly designated as `NOT NULL` can contain nulls.

Nulls

Various interpretations: unknown, missing value, inapplicable, no information...

In SQL columns that are not explicitly or implicitly designated as `NOT NULL` can contain nulls.

Behavior of nulls

- comparisons return the unknown truth value if at least one of the arguments is null
- `IS NULL` returns true
- null values counted by `COUNT(*)`, discarded by other aggregate operators.

Three-valued logic

NOT	
T	F
F	T
?	?

AND	T	F	?
T	T	F	?
F	F	F	F
?	?	F	?

OR	T	F	?
T	T	T	T
F	T	F	?
?	T	?	?

Outer joins

Outer joins

To keep the tuples in the result if there are no matching tuples in the other argument of the join:

- `LEFT`: preserve only the tuples from the left argument
- `RIGHT`: preserve only the tuples from the right argument
- `FULL`: preserve the tuples from both arguments.

The result tuples are padded with nulls.

Outer joins

To keep the tuples in the result if there are no matching tuples in the other argument of the join:

- `LEFT`: preserve only the tuples from the left argument
- `RIGHT`: preserve only the tuples from the right argument
- `FULL`: preserve the tuples from both arguments.

The result tuples are padded with nulls.

Syntax (in the `FROM` clause):

R_1 `OUTER JOIN` R_2 `ON` *Condition* `USING` *Columns*

Outer joins

To keep the tuples in the result if there are no matching tuples in the other argument of the join:

- `LEFT`: preserve only the tuples from the left argument
- `RIGHT`: preserve only the tuples from the right argument
- `FULL`: preserve the tuples from both arguments.

The result tuples are padded with nulls.

Syntax (in the `FROM` clause):

R_1 `OUTER JOIN` R_2 `ON` *Condition* `USING` *Columns*

Notes

- outer joins can be expressed using other SQL constructs
- some DBMS, e.g., Oracle, use a different syntax for outerjoins.

Limitations of relational query languages

Limitations of relational query languages

They cannot express queries involving transitive closure of binary relations:

- *"List all the ancestors of David."*
- *"Find all the buildings reachable from Bell Hall without going outside."*

Limitations of relational query languages

They cannot express queries involving transitive closure of binary relations:

- *"List all the ancestors of David."*
- *"Find all the buildings reachable from Bell Hall without going outside."*

Solution

Recursive views.

Recursion in SQL3

Recursion in SQL3

A relation R depends on a relation S if S is used, directly or indirectly, in the definition of R.

Recursion in SQL3

A relation R depends on a relation S if S is used, directly or indirectly, in the definition of R.

In a recursive view definition a relation may depend on itself!

Recursion in SQL3

A relation R depends on a relation S if S is used, directly or indirectly, in the definition of R.

In a recursive view definition a relation may depend on itself!

Recursive views in SQL

- SQL3, still unsupported in most DBMS
- recursively defined relations should be preceded by `RECURSIVE`.
- syntax:

  `WITH` R AS
  definition of R
  query to R

Example

Find all the ancestors of David:

```
WITH RECURSIVE Anc(Upper,Lower) AS
     (SELECT * FROM Parent)
  UNION
     (SELECT P.Upper, A.Lower
      FROM Parent AS P, Anc AS A
      WHERE P.Lower=A.Upper)

SELECT Anc.Upper
FROM Anc
WHERE Anc.Lower='David';
```

Example

Find all the ancestors of David:

```
WITH RECURSIVE Anc(Upper,Lower) AS
     (SELECT * FROM Parent)
  UNION
     (SELECT P.Upper, A.Lower
      FROM Parent AS P, Anc AS A
      WHERE P.Lower=A.Upper)

SELECT Anc.Upper
FROM Anc
WHERE Anc.Lower='David';
```

Stratification restriction

No view can depend on itself through negation (`EXCEPT`and the like) or aggregation.

Evaluating queries with recursive views

More involved if negation or aggregation present.

Evaluating queries with recursive views

More involved if negation or aggregation present.

Evaluation algorithm

1. Initially, the contents of all views are empty.
2. Compute the new contents of the views, using database relations and the current contents of the views.
3. Repeat the previous step until no changes in view contents occur.

Evaluating queries with recursive views

More involved if negation or aggregation present.

Evaluation algorithm

1. Initially, the contents of all views are empty.
2. Compute the new contents of the views, using database relations and the current contents of the views.
3. Repeat the previous step until no changes in view contents occur.

Why does this terminate?