## Clustering Lecture 4: Density-based Methods

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# Outline

#### • Basics

- Motivation, definition, evaluation

#### Methods

- Partitional
- Hierarchical
- Density-based
- Mixture model
- Spectral methods

#### Advanced topics

- Clustering ensemble
- Clustering in MapReduce
- Semi-supervised clustering, subspace clustering, co-clustering, etc.

# **Density-based Clustering**

#### • Basic idea

- Clusters are dense regions in the data space, separated by regions of lower object density
- A cluster is defined as a maximal set of densityconnected points
- Discovers clusters of arbitrary shape

#### Method

– DBSCAN



# **Density Definition**

- $\varepsilon$ -Neighborhood Objects within a radius of  $\varepsilon$  from an object.  $N_{\varepsilon}(p): \{q \mid d(p,q) \le \varepsilon\}$
- "High density" ε-Neighborhood of an object contains at least *MinPts* of objects.



ε-Neighborhood of *p*ε-Neighborhood of *q Density of p* is "high" (MinPts = 4) *Density of q* is "low" (MinPts = 4)

### **Core, Border & Outlier**



 $\varepsilon = 1$ unit, MinPts = 5

Given *ɛ* and *MinPts*, categorize the objects into three exclusive groups.

A point is a core point if it has more than a specified number of points (MinPts) within Eps—These are points that are at the interior of a cluster.

A border point has fewer than MinPts within Eps, but is in the neighborhood of a core point.

A noise point is any point that is not a core point nor a border point.







**Original Points** 

Point types: core, border and outliers

ε = 10, MinPts = 4

## **Density-reachability**

- Directly density-reachable
  - An object q is directly density-reachable from object p if p is a core object and q is in p's ε-neighborhood.



- q is directly density-reachable from p
- *p* is not directly density-reachable from *q*
- Density-reachability is asymmetric

#### MinPts = 4

# **Density-reachability**

- Density-Reachable (directly and indirectly):
  - A point p is directly density-reachable from  $p_2$
  - $p_2$  is directly density-reachable from  $p_1$
  - $p_1$  is directly density-reachable from q



- *p* is (indirectly) density-reachable from *q*
- q is not density-reachable from p

## **DBSCAN Algorithm: Example**

#### • Parameter

- $\varepsilon = 2 \text{ cm}$
- *MinPts* = 3



for each  $o \in D$  do if o is not yet classified then if o is a core-object then collect all objects density-reachable from oand assign them to a new cluster. else assign o to NOISE

### **DBSCAN Algorithm: Example**

- Parameter
  - $\varepsilon = 2 \text{ cm}$
  - *MinPts* = 3



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## **DBSCAN Algorithm: Example**

#### Parameter

- *ε* = 2 cm
- *MinPts* = 3



for each  $o \in D$  do if o is not yet classified then if o is a core-object then collect all objects density-reachable from oand assign them to a new cluster. else assign o to NOISE

### **DBSCAN: Sensitive to Parameters**

Figure 8. DBScan results for DS1 with MinPts at 4 and Eps at (a) 0.5 and (b) 0.4.

Figure 9. DBScan results for DS2 with MinPts at 4 and Eps at (a) 5.0, (b) 3.5, and (c) 3.0.





#### **DBSCAN: Determining EPS and MinPts**

- Idea is that for points in a cluster, their k<sup>th</sup> nearest neighbors are at roughly the same distance
- Noise points have the k<sup>th</sup> nearest neighbor at farther distance
- So, plot sorted distance of every point to its k<sup>th</sup> nearest neighbor



#### **When DBSCAN Works Well**





**Original Points** 

Clusters

- Resistant to Noise
- Can handle clusters of different shapes and sizes

#### When DBSCAN Does NOT Work Well



**Original Points** 

- Cannot handle varying densities
- sensitive to parameters—hard to determine the correct set of parameters



(MinPts=4, Eps=9.92).



(MinPts=4, Eps=9.75)

## **Take-away Message**

- The basic idea of density-based clustering
- The two important parameters and the definitions of neighborhood and density in DBSCAN
- Core, border and outlier points
- DBSCAN algorithm
- DBSCAN's pros and cons