Problem 1 (28 points)
Suppose we have EDB relations
\[
\text{frequents}(\text{Drinker}, \text{Bar}) \\
\text{serves}(\text{Bar}, \text{Beer}) \\
\text{likes}(\text{Drinker}, \text{Beer})
\]
The first indicates the bars a drinker visits; the second tells what beers each bar serves, and the last indicates which beers each drinker likes to drink. Define the following predicates using safe datalog rules.

a. (7 points) **happy**(D) that is true if drinker D frequents at least one bar that serves a beer he likes.

b. (7 points) **shouldVisit**(D, B) if bar B serves a beer drinker D likes.
c. (7 points) **veryHappy(D)** if every bar that drinker D frequents serves at least one beer he likes. You may assume that every drinker frequents at least one bar.

d. (7 points) **sad(D)** if drinker D frequents no bar that serves a beer he likes.

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**Problem 2 (28 points)**

Assume an undirected graph is represented as a set of facts of the form **node(x)** for a node x, and **edge(x, y)** and **edge(y, x)** for an edge \{x, y\}. A graph is **connected** if for every two different nodes in the graph there is a path between them. A node x is an **articulation point** of a graph if (1) the graph is connected, and (2) the graph with x and its incident edges removed is no longer connected.

a. (7 points) Write a Datalog→ (Datalog with negation) program P₁ that checks whether a given graph is connected.
b. (7 points) Write a Datalog program $P_2$ that returns the set of articulation points of a given graph.

c. (7 points) Explain why the program $P_2$ is stratified.

d. (7 points) Can the program $P_2$ be written without using negation?
Problems 3 (20 points)

Determine the containment/equivalence relationship between the following pairs of queries. Show your work. Whenever one query is contained in another, show all containment mappings. Whenever containment does not hold in a certain direction, give a counterexample to containment.

a. (10 points)
   Q1: \( p(X,Y,Z) \) :- \( e(X,Y',Z') \), \( e(X,Y,Z'') \), \( e(X',Y',Z') \), \( e(X,Y'',Z) \)
   Q2: \( p(A,B,C) \) :- \( e(A,B,D) \), \( e(A,E,C) \)

b. (10 points)
   Q1: \( p(X,Y) \) :- \( a(X,Z) \), \( a(Z,W) \), \( a(W,Y) \), \( a(Y,U) \), \( a(U,X) \)
   Q2: \( p(X,Y) \) :- \( a(X,Y) \), \( X \geq Y \)
Problem 4 (24 points)

Consider a Local-As-View integration system that has one global predicate \( p \), and the following two views:

\[
\begin{align*}
v(X,Y) & : - p(X,Y), p(Y,Z) \\
w(U,V) & : - p(W,U), p(U,V)
\end{align*}
\]

The query to be answered is:

\[
q(A,B) : - p(A,C), p(C,B)
\]

Find the maximally contained rewriting of query Q using the MiniCon algorithm. Make sure that you show the following:

1. The MiniCon descriptions (MCDs) and the containment mappings for each one
2. All possible rewritings, where the views are not unfolded
3. Optimize the rewritings, both individually and collectively, and give the final maximally contained rewriting