

The Strategies So Far, version II (more to come!)

Notes:

1. Numbering corresponds to my lectures of 11 and 16 November.
 2. Strategies are listed in “quasi-logical” order.
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4: Determine precondition Q and postcondition R (if not already known)

4.1: Use initial and final values of variables to help determine pre- and postconditions.

1: Look at the *goal* (i.e., the postcondition) of the program.

2: Refine the postcondition until it’s usable; e.g., replace high-level concepts with their definitions.

3: Suppose we know a precondition Q for an IF.

Then: to develop a guarded command for IF, do:

repeat:

(a) find a command S_i such that $S_i\{R\}$, at least sometimes

3.1: choose an S_i that: (i) is suggested by R (cf. strategy 1)
and (ii) is simple

5: Look at the precondition for clues to find a command S_i such that $S_i\{R\}$.

5.1: If precondition is part of postcondition, use *skip*.

(b) find a Boolean guard B_i such that $B_i \Rightarrow wp(S_i, R)$ (then use: $B_i \rightarrow S_i$)

3.2: compute $wp(S_i, R)$ and try $B_i = wp(S_i, R)$

6: By Thm 10.5, each guard B_i must satisfy $Q \wedge B_i \Rightarrow wp(S_i, R)$

\therefore if Q and $wp(S_i, R)$ are known, can determine B_i as whatever must be
conjoined to Q to imply $wp(S_i, R)$

or

(a') suppose you have guards B_1, \dots, B_{i-1} ;
find B_i such that $Q \Rightarrow (B_1 \vee \dots \vee B_i)$

(b') find S_i such that $Q \wedge B_i \Rightarrow wp(S_i, R)$

until $Q \Rightarrow (B_1 \vee \dots \vee B_n)$ (recall Thm 10.5!)

7: All other things being equal, make the guards of an IF as *strong* as possible
(so that errors will cause the program to abort, rather than work in a GIGO manner).

To develop a DO-program, given:

- precondition Q ,
- invariant P ,
- bound function t ,
- and postcondition R :

8. Find an initialization that makes P true before the loop.

9.1 Find a guard B such that $P \wedge \neg B \Rightarrow R$;

9.2 develop body S that (a) decrements t
while (b) preserving P

10. All other things being equal, make the guards of a DO-loop as *weak* as possible
(so that errors will cause ∞ loops rather than going undetected).