

Hw1 Solution

1. Convert the decimal number to Binary and Hexadecimal values

a. $529 \div 16 = 33 \text{ - } 1$

$$33 \div 16 = 2 \text{ - } 1$$

$$= 529_{10} = 0010\ 0001\ 0001$$

b. $24.275 = 0001\ 1000 . 0100\ 0110\ 0110\ 0110\ 0110$

2. Express the following numbers in decimal a. $(1010.11)_2$ b. $(9ABC.A)_{16}$

10.75

3. Perform subtraction by 2's complementing the subtrahend and adding. Assume the numbers to be of 8 bits

a. $(1000\ 1101)_2 - (1\ 0010)_2 \quad 1000\ 1101 + 1110\ 1110 = 0111\ 1011$

b. $(1\ 0010)_2 - (1000\ 1101)_2 \quad 0001\ 0010 + 0111\ 0011 = 1000\ 0101 = -7_B$

4. Write the expression "SOS 16" in ASCII, using an eight-bit code. Include the space. Treat the left most bit of each character as a parity bit. Each 8-bit code should have even parity

$$\text{SOS } 16 = 101\ 0011\ 100\ 1111\ 101\ 0011\ 010\ 0000\ 011\ 0001\ 011\ 0110$$

$$\text{With even parity} = 0101\ 0011\ 1100\ 1111\ 0101\ 0011\ 1010\ 0000\ 1011\ 0001\ 0011\ 0110 =$$

In Hex - 53 CF 53 A0 B1 36

5.

1.30 73 F4 E5 76 E5 4A EF 62 73

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73:  0_111_0011  s
F4:  1_111_0100  t
E5:  1_110_0101  e
76:  0_111_0110  v
E5:  1_110_0101  e
4A:  0_100_1010  j
EF:  1_110_1111  o
62:  0_110_0010  b
73:  0_111_0011  s
    
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(upper case J in Problem 30) b) odd parity

6. Minimize the following Boolean expression to minimum number of literals

a) $(x+y+z')(x'y+z)$

$$xz+x'y+yz+x'yz' = xz +x'y +yz = xz + x'y$$

b) $w'xy + wxy' + wxy + w'xy' = w'x+wx = x$

7. We can perform logical operations on strings of bits by considering each pair of corresponding bits separately (called bitwise operation). Given two sixteen-bit strings $A = (FOOF)_{16}$ and $B = (FO)_{16}$, evaluate the sixteen-bit result after the following logical operations:

(a) $A \text{ AND } B \quad FOOF \text{ AND } 00F0 = 0000$

(b) $A \text{ OR } B \quad FOOF \text{ AND } 00F0 = FOFF$

(c) A XOR B F00F XOR 00F0 = F0FF

(d) NOT A 0FF0

(e) NOT B FF0F

8.

(d) $bd' + acd' + ab'c + a'c' = \Sigma (0, 1, 4, 5, 10, 11, 14)$

$$F' = \Sigma (2, 3, 6, 7, 8, 9, 12, 13, 15)$$

$$F = \Pi (0, 2, 3, 6, 7, 8, 12, 13, 15)$$

abcd	F
0000	1
0001	1
0010	0
0011	0
0100	1
0101	1
0110	0
0111	0
1000	0
1001	0
1010	1
1011	1
1100	1
1101	0
1110	1
1111	0

9.

2.21 (a) $F(x, y, z) = \Sigma(1, 3, 5) = \Pi(0, 2, 4, 6, 7)$

(b) $F(A, B, C, D) = \Pi(3, 5, 8, 11) = \Sigma(0, 1, 2, 4, 6, 7, 9, 10, 12, 13, 14, 15)$

10. Complement the following function using DeMorgan's theorem. $f = ((A+B'C)'C + AB'C + A)'$

$$F = ((A+B'C)'C)' \cdot (AB'C)' \cdot (A)'$$

$$= ((A+B'C) + C)' \cdot (A'+B+C)' \cdot A$$

$$= (A+B'C+C)(A'+B+C)A$$