CSE 250 Data Structures

Dr. Eric Mikida epmikida@buffalo.edu 208 Capen Hall

Lec 15: Stacks and Queues

Announcements

• Midterm #1 on Friday

Recap

Stacks: Last In First Out (LIFO)

- Push (put item on top of the stack)
- Pop (take item off top of stack)
- Peek (peek at top of stack)

Queues: First in First Out (FIFO)

- Enqueue (put item on the end of the queue)
- Dequeue (take item off the front of the queue)
- Peek (peek at the front of the queue)

Thought Question: How could you use an array to build a queue?

```
public class ArrayQueue<E> extends Queue<E> {
     private ArrayList<E> data;
 3
     public void add(E value) { // enqueue
4
       data.add(value);
6
     public E remove() { // dequeue
       return data.remove(0);
9
10
     public E peek() {
11
       return data.get(0);
12
13
```

```
public class ArrayQueue<E> extends Queue<E> {
     private ArrayList<E> data;
     public void add(E value) { // enqueue
4
       data.add(value); _____
                                           Amortized \Theta(1)
6
     public E remove() { // dequeue
       return data.remove(0);
                                          \Theta(n):(
10
     public E peek() {
       return data.get(0);
11
                                         \Theta(1)
12
13
```

```
public class ArrayQueue<E> extends Queue<E> {
     private ArrayList<E> data;
 3
     public void add(E value) { // enqueue
4
       data.add(0, value);
6
     public E remove() { // dequeue
       return data.remove(data.size() - 1);
10
     public E peek() {
11
       return data.get(data.size() - 1);
12
13
```

```
public class ArrayQueue<E> extends Queue<E> {
     private ArrayList<E> data;
     public void add(E value) { // enqueue
4
       data.add(0, value); _____
                                              \Theta(n):(
6
     public E remove() { // dequeue
       return data.remove(data.size() - 1);
                                                          \Theta(1)
10
     public E peek() {
       return data.get(data.size() - 1);
                                                       \Theta(1)
12
13
```

Can we avoid the cost of moving all of the elements forward or backward each time we add or remove?

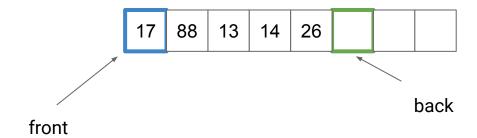
Can we avoid the cost of moving all of the elements forward or backward each time we add or remove?

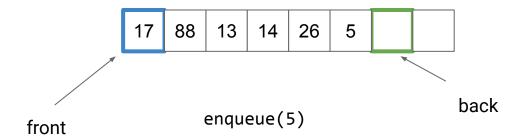
Why didn't we have to pay that cost with a list?

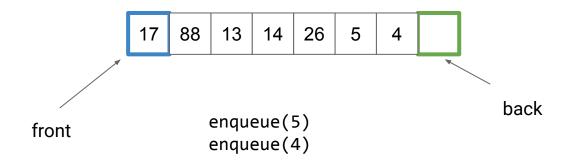
Can we avoid the cost of moving all of the elements forward or backward each time we add or remove?

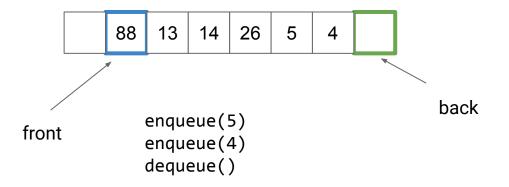
Why didn't we have to pay that cost with a list?

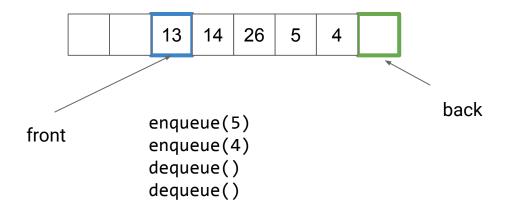
Update our values of "first" and "last"!

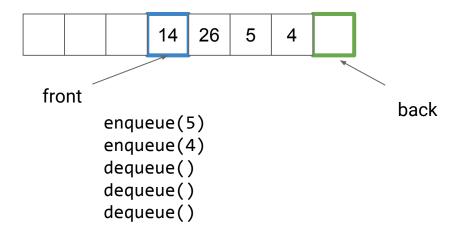


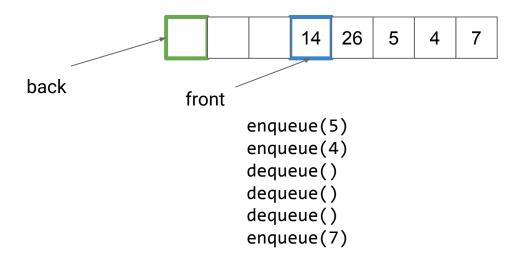


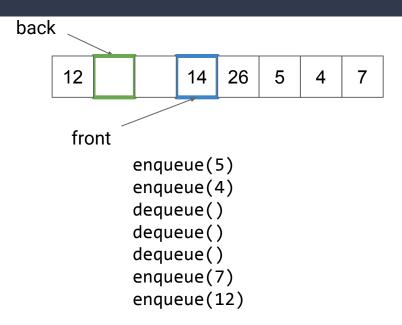


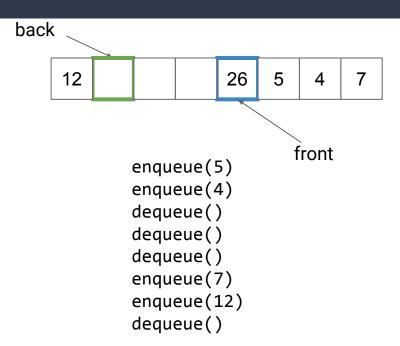


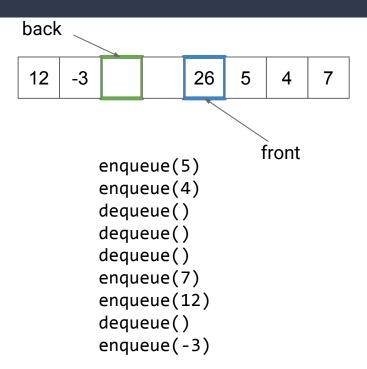












ArrayDeque (Resizable Ring Buffer)

Active Array = [start, end)

Enqueue

- Resize buffer if needed
- 2. Add new element at buffer[end]
- 3. Advance end pointer (wrap to front as needed)

Dequeue

- 1. Remove element at buffer[start]
- 2. Advance start pointer (wrap to front as needed)

ArrayDeque (Resizable Ring Buffer)

Active Array = [start, end)

Enqueue

- 1. Resize buffer if needed
- 2. Add new element at buffer[end]
- 3. Advance end pointer (wrap to front as needed)

Dequeue

- 1. Remove element at buffer[start]
- 2. Advance start pointer (wrap to front as needed)

ArrayDeque (Resizable Ring Buffer)

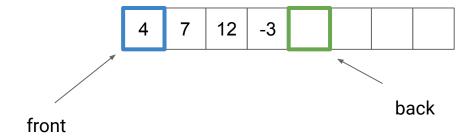
Active Array = [start, end)

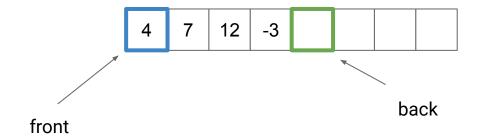
Enqueue Amortized $\Theta(1)$

- 1. Resize buffer if needed
- 2. Add new element at buffer[end]
- 3. Advance end pointer (wrap to front as needed)

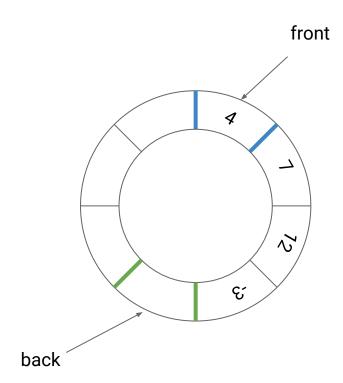
Dequeue $\Theta(1)$

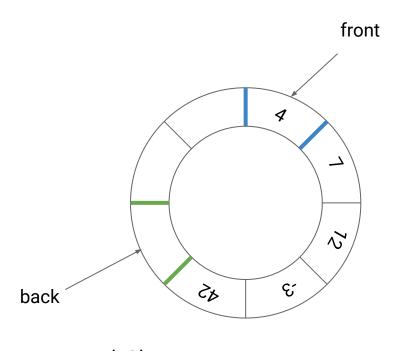
- 1. Remove element at buffer[start]
- 2. Advance start pointer (wrap to front as needed)



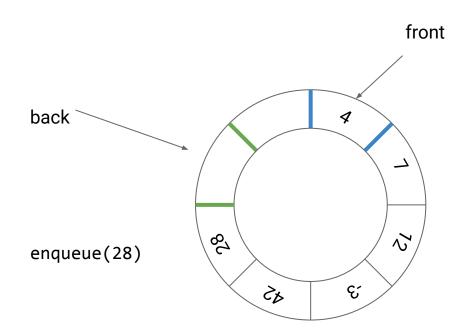


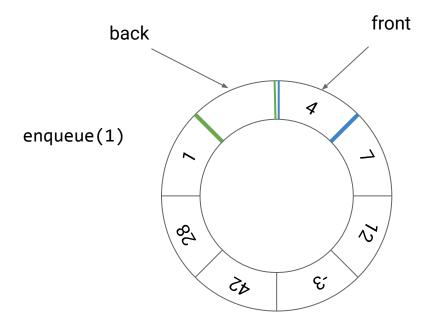
Conceptually, we can think of this as a ring...

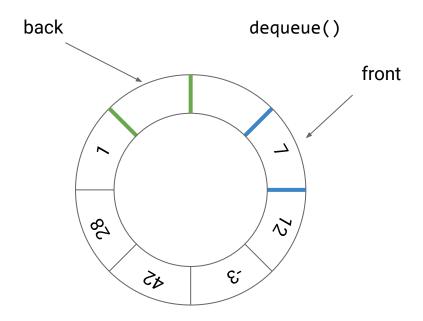


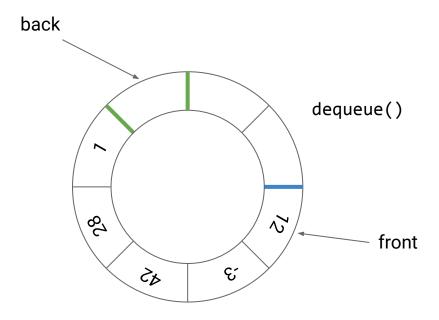


enqueue(42)









Applications of Stacks and Queue

Stack: Checking for balanced parentheses/braces

Queue: Scheduling packets for delivery

Both: Searching mazes

Balanced Parentheses/Braces

What does it mean for parentheses/braces to be balanced?

- 1. Every opening symbol is matched by a closing symbol
 - 2. No nesting overlaps (ie {(}) is not ok).

$$\{()(\{\})\}\ \{())\ ())$$

Balanced Parentheses/Braces

What does it mean for parentheses/braces to be balanced?

Every opening symbol is matched by a closing symbol
 No nesting overlaps (ie {(}) is not ok).

 $\{()(\{\})\}\ \{())\ ()\}$



Balanced Parentheses/Braces

What does it mean for parentheses/braces to be balanced?

Every opening symbol is matched by a closing symbol
 No nesting overlaps (ie {(}) is not ok).

{()({})} {()) ())

Balanced Parentheses/Braces

What does it mean for parentheses/braces to be balanced?

Every opening symbol is matched by a closing symbol
 No nesting overlaps (ie {(}) is not ok).

Idea #1

Idea: Count the number of unmatched open parens/braces.

Increment counter on (, decrement on)

Idea #1

Idea: Count the number of unmatched open parens/braces.

Increment counter on (, decrement on)

Problem: allows for {(})

Idea #2

Idea: Track nesting on a stack!

On (or {, push the symbol on the stack.

On) or }, pop the stack and check for a match.

Demo from last fall:

[https://odin.cse.buffalo.edu/teaching/cse-250/2022fa/slide/14b-QueueStackApps.html#/13]

Network Packets

Router: 1gb/s internal network, 100mb/s external

- 1 gb/s sent to the router, but only 100mb/s can leave.
- How do we handle this?

Queues

- Enqueue data packets in the order they are received.
- When there is available outgoing bandwidth, dequeue and send.

Avoiding Queueing Delays

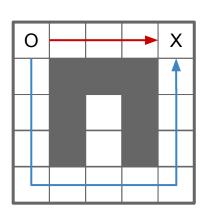
Limit size of queue; Packets that don't fit are dropped

TCP: blocked packets are retried

UDP: application deals with dropped packets

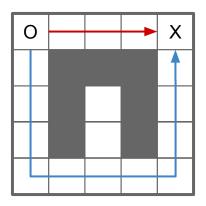
O is the start, X is the objective

- There may be multiple paths
- Generally, we want the shortest



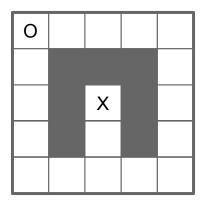
Approach 1: Take the first available route in one direction

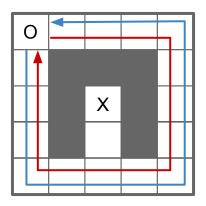
- Right, Down, Left, or Up
- Down, Right, Up, or Left



How do you know which one is best?

Is there anything wrong with this algorithm?





Priority order doesn't guarantee exploring the entire maze

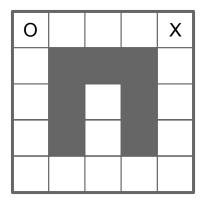
Formalizing Maze-Solving

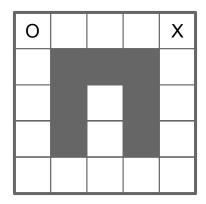
Inputs:

- The map: an n x m grid of squares which are either filled or empty
- The **O** is at position *start*
- The **X** is at position *dest*

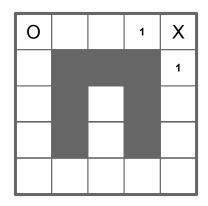
Goal: Compute steps(start, dest), the minimum number of steps from start to end.

How do we define the steps function?

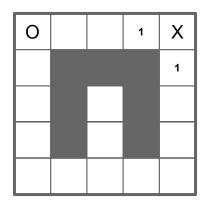




How many steps are required for the squares right next to X?

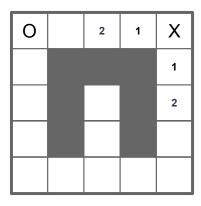


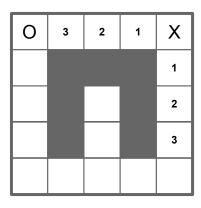
How many steps are required for the squares right next to X?

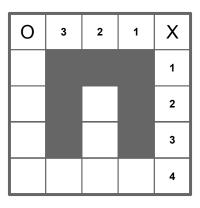


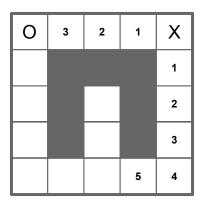
How many steps are required for the squares right next to X?

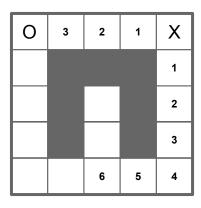
And the squares next to those?

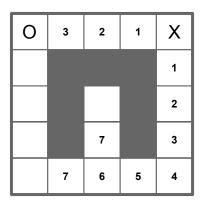


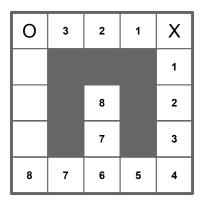


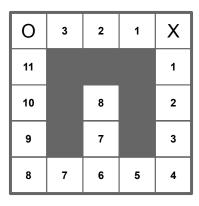


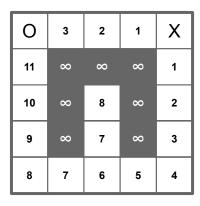


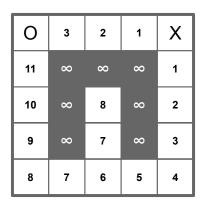




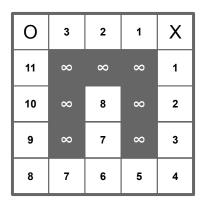






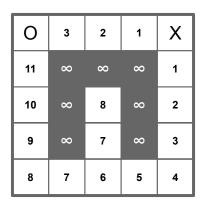


So what is the number of steps from O to X?

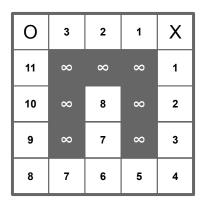


So what is the number of steps from O to X?

4 (min of neighbors + 1)



Does this solution remind you of anything?



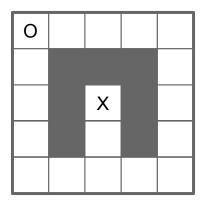
Does this solution remind you of anything?

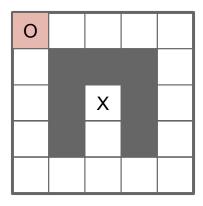
Recursion!

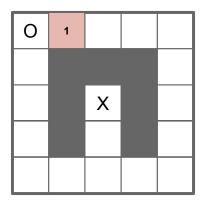
$$steps(\texttt{pos}, \texttt{dest}) = \begin{cases} 0 & \text{if pos} = \texttt{dest} \\ \infty & \text{if } is_filled(\texttt{pos}) \\ 1 + min_adjacent(\texttt{pos}, \texttt{dest}) & \textbf{otherwise} \end{cases}$$
 where...

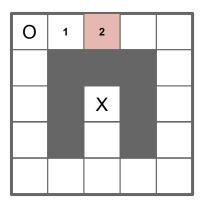
$$min_adjacent(\texttt{pos},\texttt{dest}) = \min \begin{cases} steps(moveRight(\texttt{pos}),\texttt{dest}) \\ steps(moveDown(\texttt{pos}),\texttt{dest}) \\ steps(moveLeft(\texttt{pos}),\texttt{dest}) \\ steps(moveUp(\texttt{pos}),\texttt{dest}) \end{cases}$$

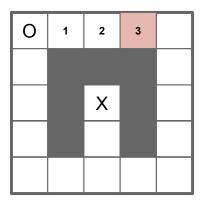
```
steps(pos, dest):
  if pos == dest then return 0
  elif is filled(pos) then return ∞
  else return 1 + min of
    steps(moveRight(pos, dest))
    steps(moveDown(pos, dest))
    steps(moveLeft(pos, dest))
    steps(moveUp(pos, dest))
```

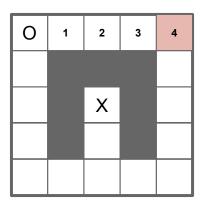


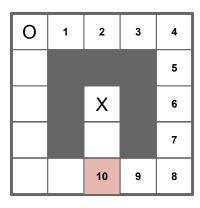


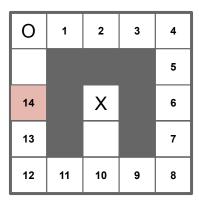


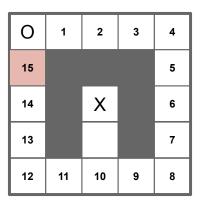


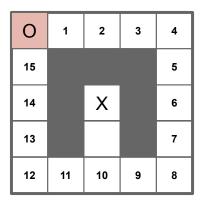


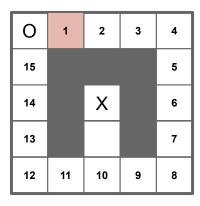


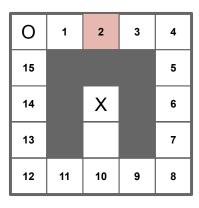


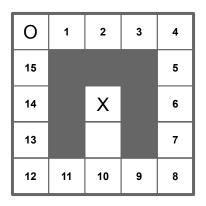




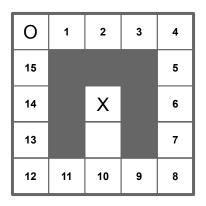








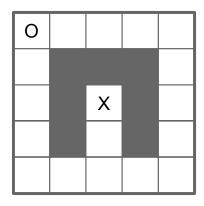
Problem: Infinite loop!

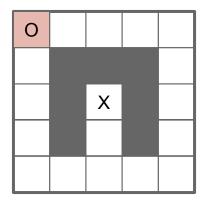


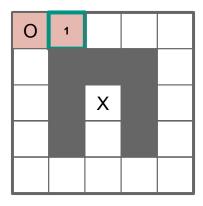
Problem: Infinite loop!

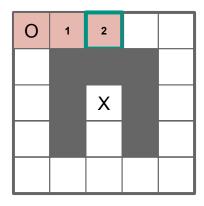
Insight: A path with a loop in it can't be shorter than one without the loop

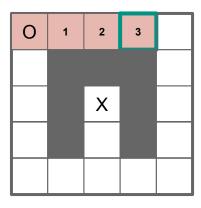
```
steps(pos, dest):
   if pos == dest then return 0
   elif is_visited(pos) then return ∞
   elif is_filled(pos) then return ∞
   else
     Mark pos as visited
     return 1 + min of all 4 steps
```

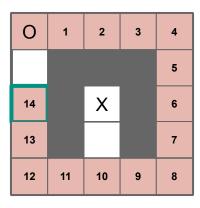


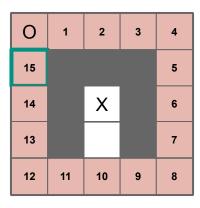


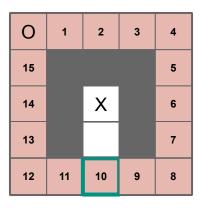


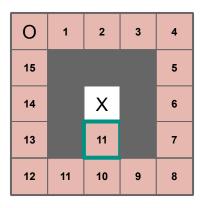


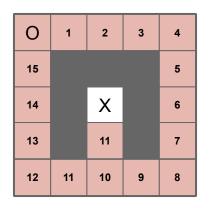




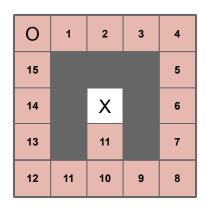








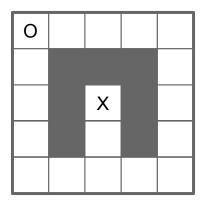
Problem: The first time you visit a node may be from a longer path!

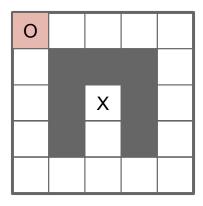


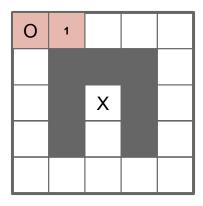
Problem: The first time you visit a node may be from a longer path!

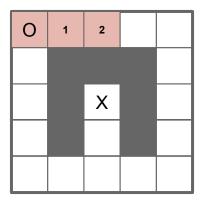
Insight: Unmark nodes as you leave them

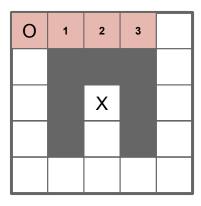
```
steps(pos, dest):
 if pos == dest then return 0
  elif is visited(pos) then return ∞
  elif is filled(pos) then return ∞
  else
    Mark pos as visited
    min = 1 + min of all 4 steps
    Mark pos as unvisited
    return min
```

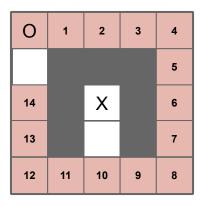


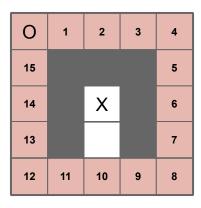


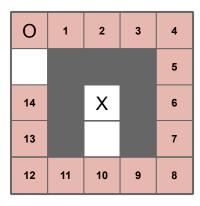


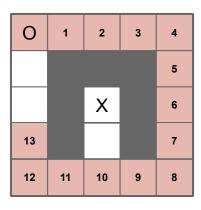


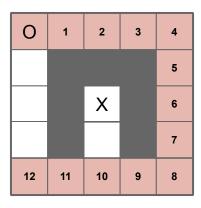


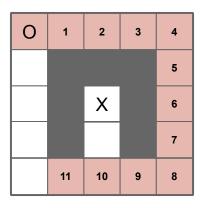


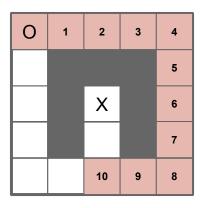


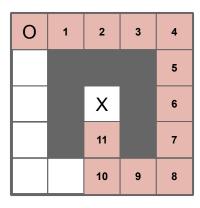


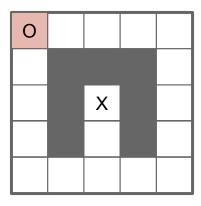


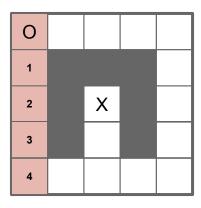


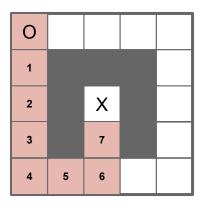












Formalizing Maze-Solving

Inputs:

- The map: an n x m grid of squares which are either filled or empty
- The **O** is at position *start*
- The **X** is at position *dest*

Goal: Compute steps(start, dest), the minimum number of steps from start to end.

Formalizing Maze-Solving

Inputs:

- The map: an n x m grid of squares which are either filled or empty
- The **O** is at position *start*
- The **X** is at position *dest*

Goal: Compute steps(start, dest), the minimum number of steps from start to end. ✓

Formalizing Maze-Solving

Inputs:

- The map: an n x m grid of squares which are either filled or empty
- The O is at position start
- The **X** is at position *dest*

Goal: Compute steps(start, dest), the minimum number of steps from start to end. ✓

Idea: Keep track of the nodes marked visited...that's our path!

Mazes: Now with...some data structure?

```
steps(pos, dest, visited):
  if pos == dest then return visited.copy()
  elif pos ∈ visited then return no path
  elif is filled(pos) then return no path
  else
   visited.append(pos)
    bestPath = 1 + min of all 4 steps
   visited.removeLast()
    return bestPath
```

Mazes: Now with...some data structure?

```
steps(pos, dest, visited):
  if pos == dest then return visited.copy()
  elif pos ∈ visited then return no path
  elif is_filled(pos) then return no path
  else
                                            What could this data
    visited.append(pos) ~
                                            structure be??
    bestPath = 1 + min of all 4 steps
    visited.removeLast()
    return bestPath
```

Mazes: Now with...Stacks!

```
steps(pos, dest, visited):
  if pos == dest then return visited.copy()
  elif pos ∈ visited then return no path
  elif is filled(pos) then return no path
  else
                                          A stack!
    visited.push(pos)
    bestPath = 1 + min of all 4 steps
    visited.pop()
    return bestPath
```

Queues?

Thought Experiment: Can we do something similar with queues?