

①
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$$F1(x,y) = xy + x'$$

$$F2(x,y,z) = xy + yz + zx'$$

Explain a two-variable function
Describe Truth Table

Input 1 col / input

input		
x	y	F1
0	0	1
0	1	1
1	0	0
1	1	1

all the patterns of xy

Output function

x, y binary variable

$$F1 = x \cdot y + x'$$

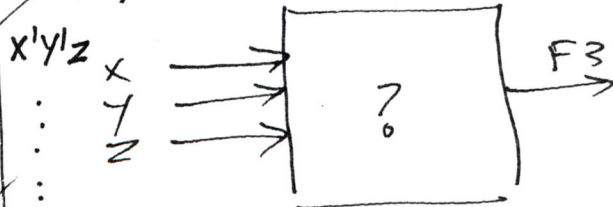
or

00	$0 \cdot 0 + 1 = 0 + 1 = 1$
01	$0 \cdot 1 + 1 = 0 + 1 = 1$
10	$1 \cdot 0 + 0 = 0 + 0 = 0$
11	$1 \cdot 1 + 0 = 1 + 0 = 1$

3-variable function

	x	y	z	F3 output
m ₀	0	0	0	0
m ₁	0	0	1	1 ✓
m ₂	0	1	0	0
m ₃	0	1	1	0
m ₄	1	0	0	1 ✓
m ₅	1	0	1	1 ✓
m ₆	1	1	0	1 ✓
m ₇	1	1	1	1 ✓

$$x' \cdot y' \cdot z' = x' y' z'$$



$F3(x,y,z) =$ Sum of minterms notation

$$m_1 + m_4 + m_5 + m_6 + m_7$$

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$$F_3(x, y, z) = \sum (1, 4, 5, 6, 7)$$

Sum of minterms

Boolean expression

Boolean variables

Boolean terms

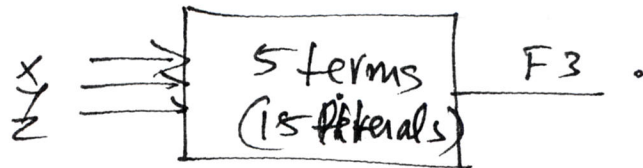
$$F_3(x, y, z) = \sum (1, 4, 5, 6, 7)$$

$$= \cancel{x y z} + \dots$$

$$= x'y'z + xy'z' + xy'z + xyz' + xyz$$

→ F_3 has 5 terms

F_3 has $5 \times 3 = 15$ literals



minimize

↓ terms

minimize

↓ literals

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$$F(x, y, z) = x'y'z + \underbrace{x y' z' + x y' z + x y z'}_{\text{circled}} + \underline{\underline{x y z}}$$

Boolean Algebraic Simplification

"factorize" "common"

$$\Rightarrow z \cdot (\cancel{x'y'} + \cancel{x y'} + \cancel{x y})$$

$$= x (y'z' + y'z + yz' + yz) + x'y'z$$

$$= x \cancel{(y'(z' + z) + y(z' + z))} + x'y'z$$

$$= x (y' \cdot 1 + y \cdot 1) + x'y'z$$

$$= x (\cancel{y' + y}) + x'y'z$$

$$= \underline{x + x'y'z} \quad \text{Distributive law}$$

$$= (\cancel{x + x'}) \cdot (x + y'z)$$

$$= \underline{1 \cdot (x + y'z)} = \underline{\underline{x + y'z}}$$

