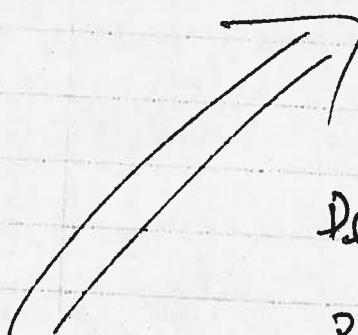


Oct 23, 2015

CSE 241

## Finite State Machine FSM



tool

Design of a sequential circuit

Problem that has "state"

program

~~Memory~~  
MEMORY

Java

Python

any lang.

US Football

FSM Five-tuple

{ initial state, final state, set of states, set of transitions, symbols/triggers that bring about the transition }

1. Two teams

2. Set of input symbols { 1, 2, 3, 6 }  
initial  $S_0$  →  $S_{score}$  ... →  $S_x$

2A  
2B  
2C

↑ ↗ ↗

→  $S_x$

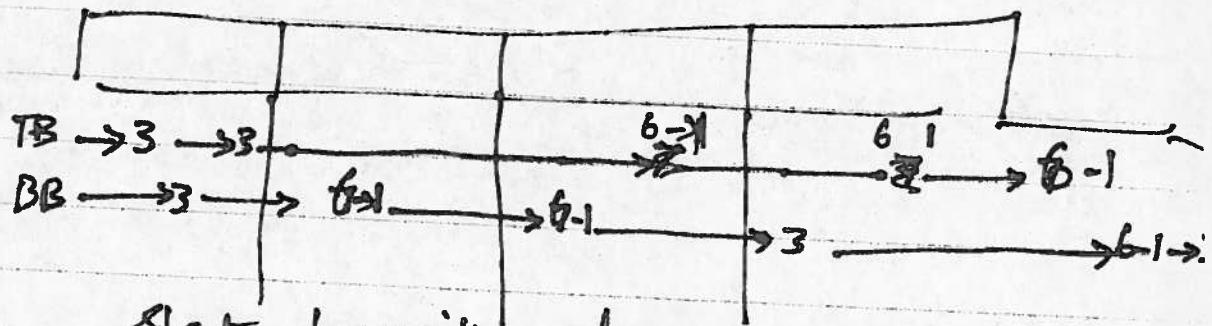
3. State diagram transitions

Two teams: Buffalo Bills (BB)

Oct 23, 2011  
②

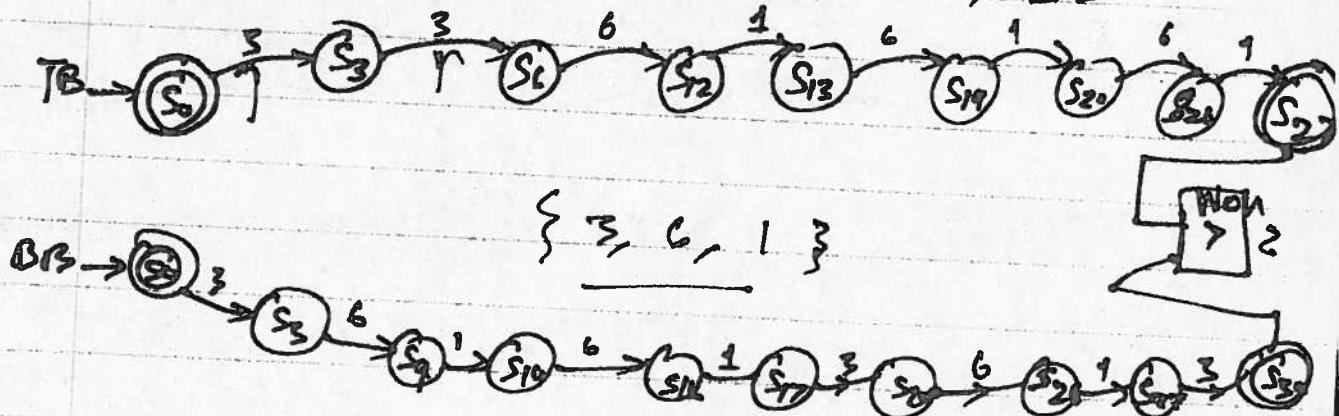
Tam Bay Buccaneers (TB)

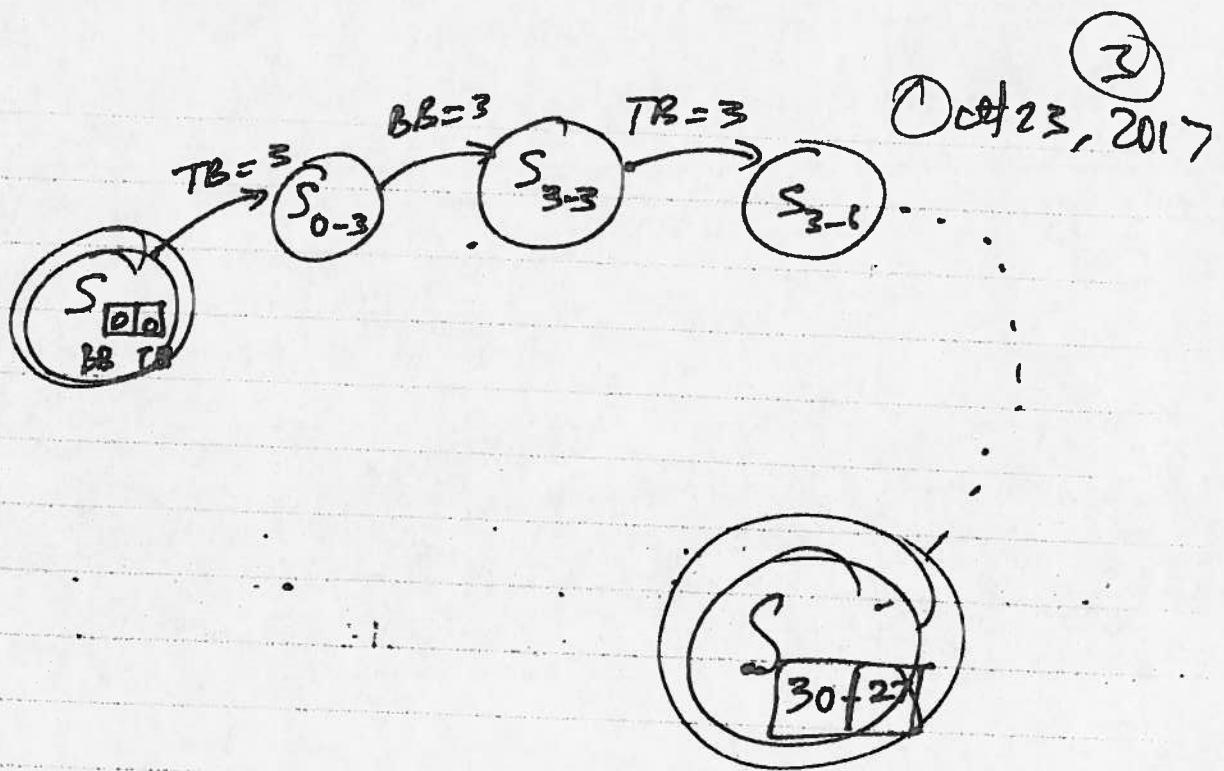
### Scoring History:



State transition diagram:

Design 1: Two instances: TB - BB





Oct 25, 2017  
①

1. How to submit Lab on ublearns.
2. Academic Integrity
  - Individual labs
  - List of 'No's

## 2. Sequential circuit design

## language recognition

Design a sequential circuit for recognizing pattern 1001 in an input string (x) of 0's and 1's. Use D-FF and provide the complete design. Show all the steps.

$\uparrow$  small pattern

X 10 10 10 0 0 0 0 0 1001  
~~XXXXXX~~ X X X X X X ↑↑↑↑↑↑

Y . . . . . . . . . . . . . . . 1

Analyze Y  
Design word problem

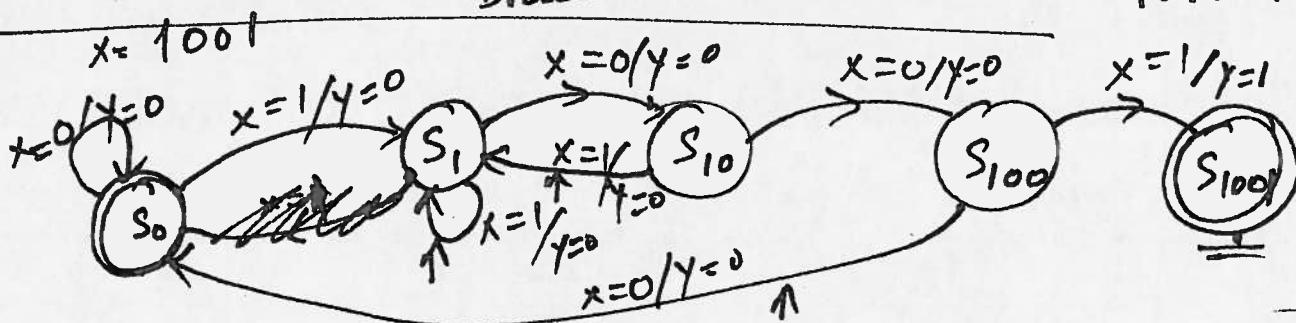
Finite state machine

characteristic table

FF input equations

Draw the circuit

11001  
101001



Case1: 11001

Case2: 101001

Case3: 10001001

0000100100000001001

non-overlapping  
pattern

"State reduction"

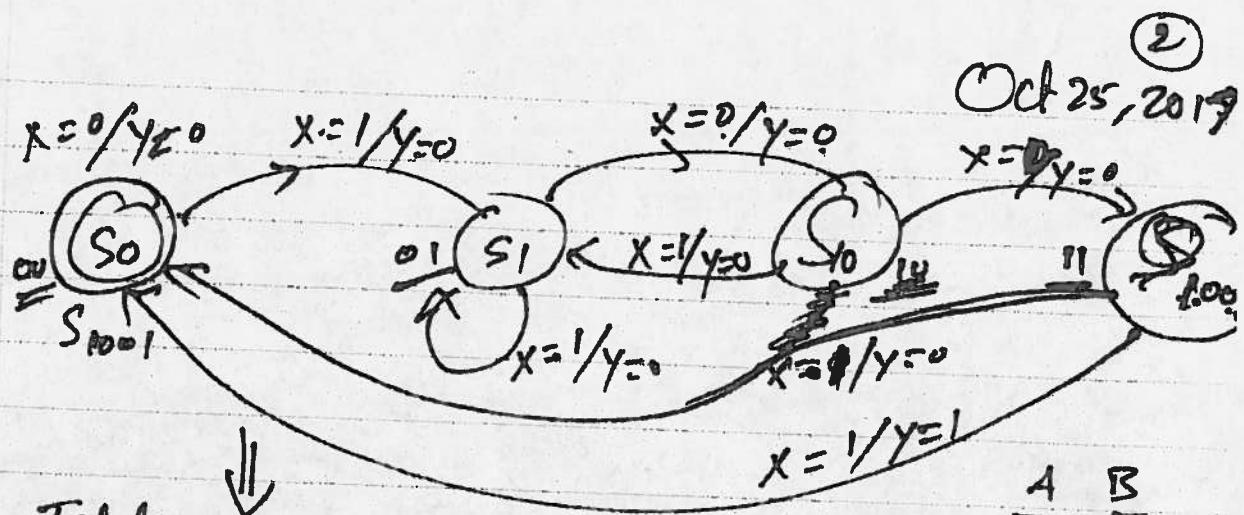


Table:

Current state $A(t)$ $B(t)$	input x	next state $A(t+1)$ $B(t+1)$	Output FF inputs $y$	FF input output $DA$ $DB$
0 0	0	0 0	0	0 0
0 0	1	0 1	0	0 1
0 1	0	1 0	0	0 0
0 1	1	0 1	0	1 0
1 0	0	1 1	0	1 1
1 0	1	0 1	0	0 1
1 1	0	0 0	0	0 1
1 1	1	0 0	1	0 0

FF input equations:

$$DA = ?$$

$$DB = ?$$

	00	01	11	10
0	0	0	0	1
1	1	0	0	0

	00	01	11	10
0	0	0	0	0
1	1	1	0	0

$$\begin{aligned} DA &= A \oplus B \cdot x + A \bar{B} \\ &= B(A'x + Ax) \end{aligned}$$

$$DB = A \oplus B + B \cdot x + A'x$$

(2)

Oct. 27, 201

... continuation of 1001 recognizer.

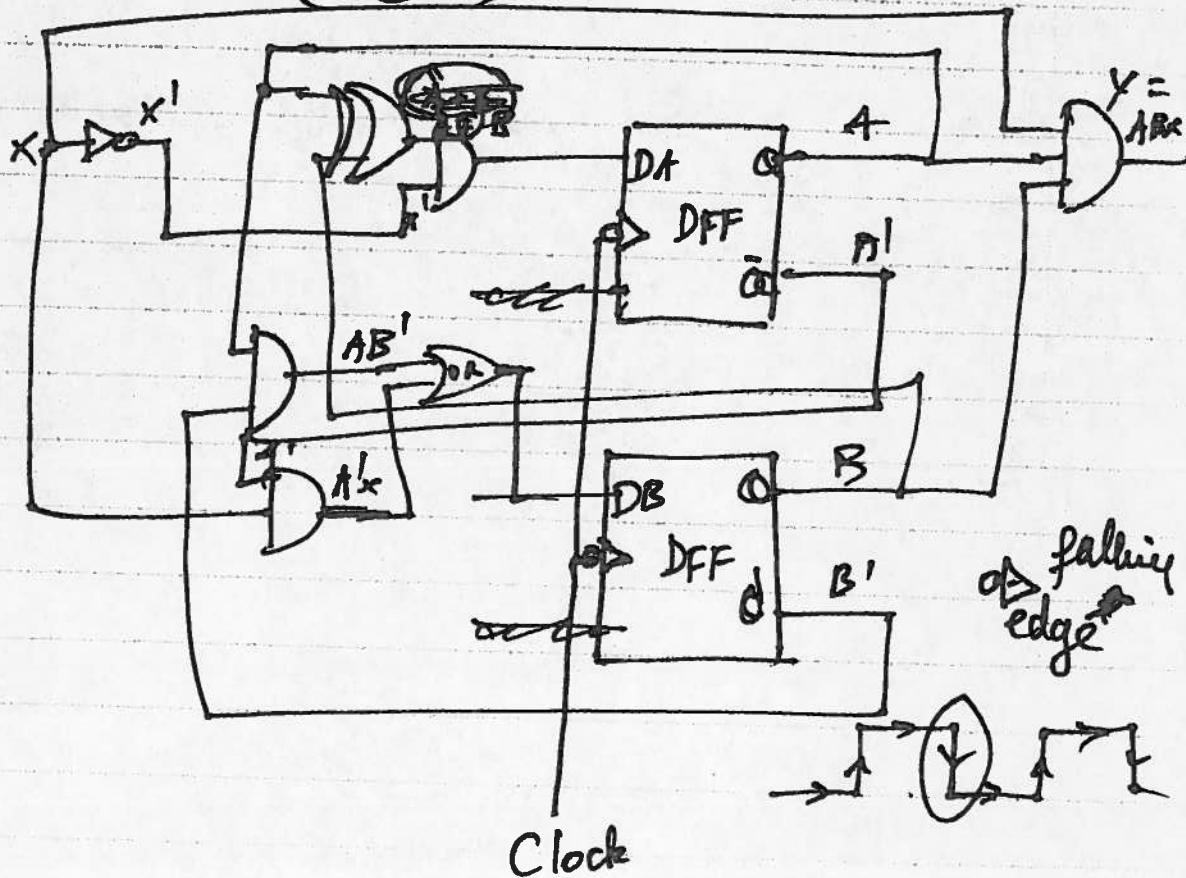
FF input equations:  $D_A = ?$   $D_B = ?$

$A$	$B$	$x$	$D_A$
0	0	0	0
0	1	0	1
1	0	1	0
1	1	0	1

$A$	$B$	$x$	$D_B$
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

$$\begin{aligned}
 D_A &= A B' x' + A' B x' \\
 &= x' (A B' + A' B) \\
 &= x' (A \oplus B)
 \end{aligned}$$

$$D_B = A B' + A' x$$



Problem: Design a counter <sup>3</sup> <sub>Oct. 2017</sub>  
that counts with a sequence

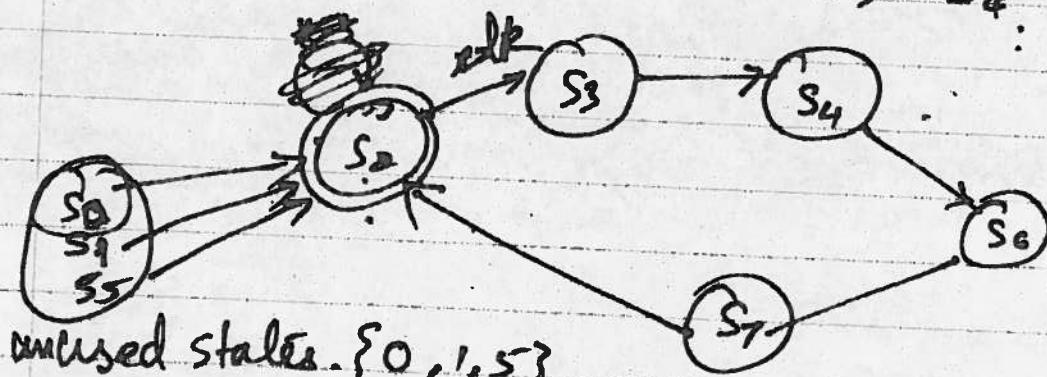
$\{0, 1, 5\}$

in T-FF.

$\{2, 3, 4, 6, 7\}$

$\{010, 011, 100, 110, 111\}$

$S_2 \quad S_3 \quad S_4 \quad S_5 \quad S_6 \quad S_7$



unused states.  $\{0, 1, 5\}$

	A(t)	B(t)	C(t)		A(t+1)	B(t+1)	C(t+1)		T <sub>A</sub>	T <sub>B</sub>	T <sub>C</sub>
S <sub>0</sub>	0	0	0		0	1	0		0	1	0
S <sub>1</sub>	0	0	1		0	1	0		0	1	1
S <sub>2</sub>	0	1	0		0	1	1		0	0	1
S <sub>3</sub>	0	1	1		1	0	0		1	1	1
S <sub>4</sub>	1	0	0		1	0	0		0	1	0
S <sub>5</sub>	1	0	1		0	1	0		1	1	1
S <sub>6</sub>	1	1	0		1	1	1		0	0	1
S <sub>7</sub>	1	1	1		0	1	0		1	0	1

FF equations:

$$T_A = ? \quad T_B = ? \quad T_C = ?$$

		BC					
		00	01	11	10		
A	B	0	0	1	0		
		1	0	1	0		

$T_A(A, B, C)$

		B'					
		00	01	11	10		
A	B	0	1	1	0		
		1	1	0	0		

$T_B(A, B, C, B')$

		BC					
		00	01	11	10		
A	B	0	0	1	1		
		1	0	1	1		

$T_C(A, B, C, B')$

$$\bar{T}_A = AC + BC \quad \bar{T}_B = B' + A'C$$

$$T_C = C + B$$

